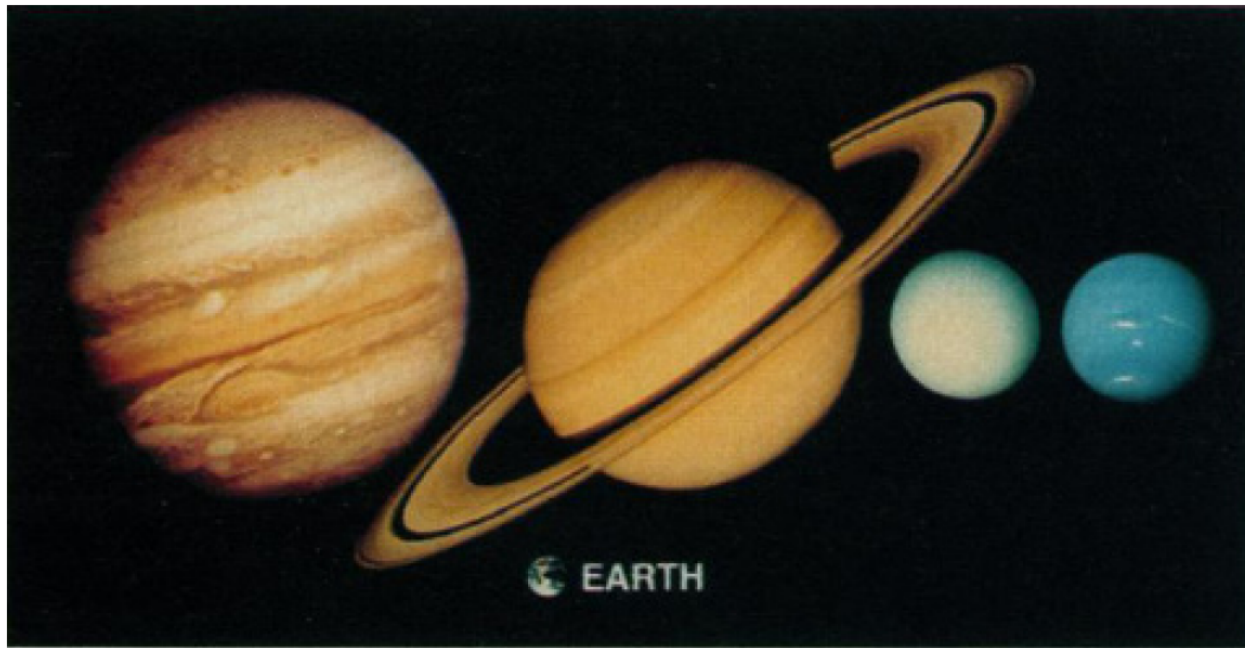
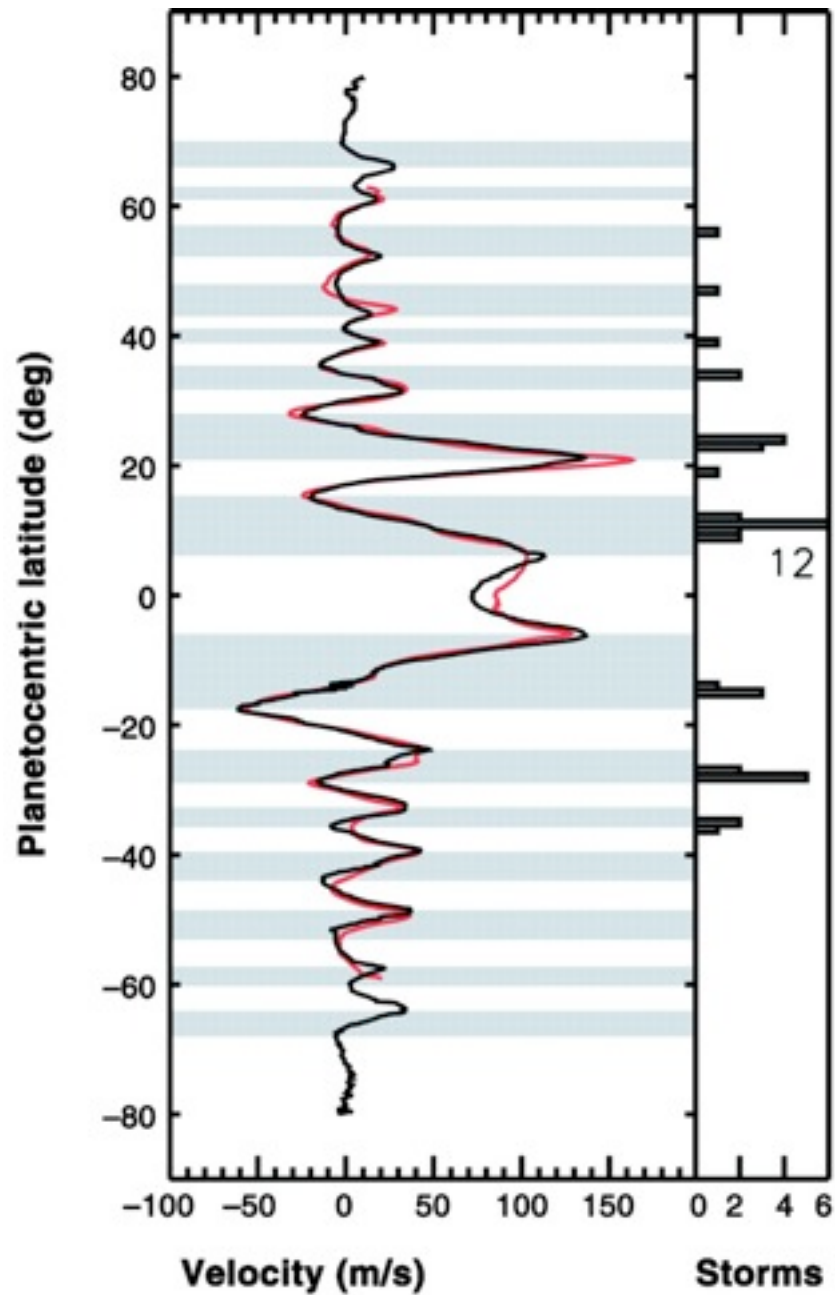


Mechanisms of Jet Formation on the Giant Planets



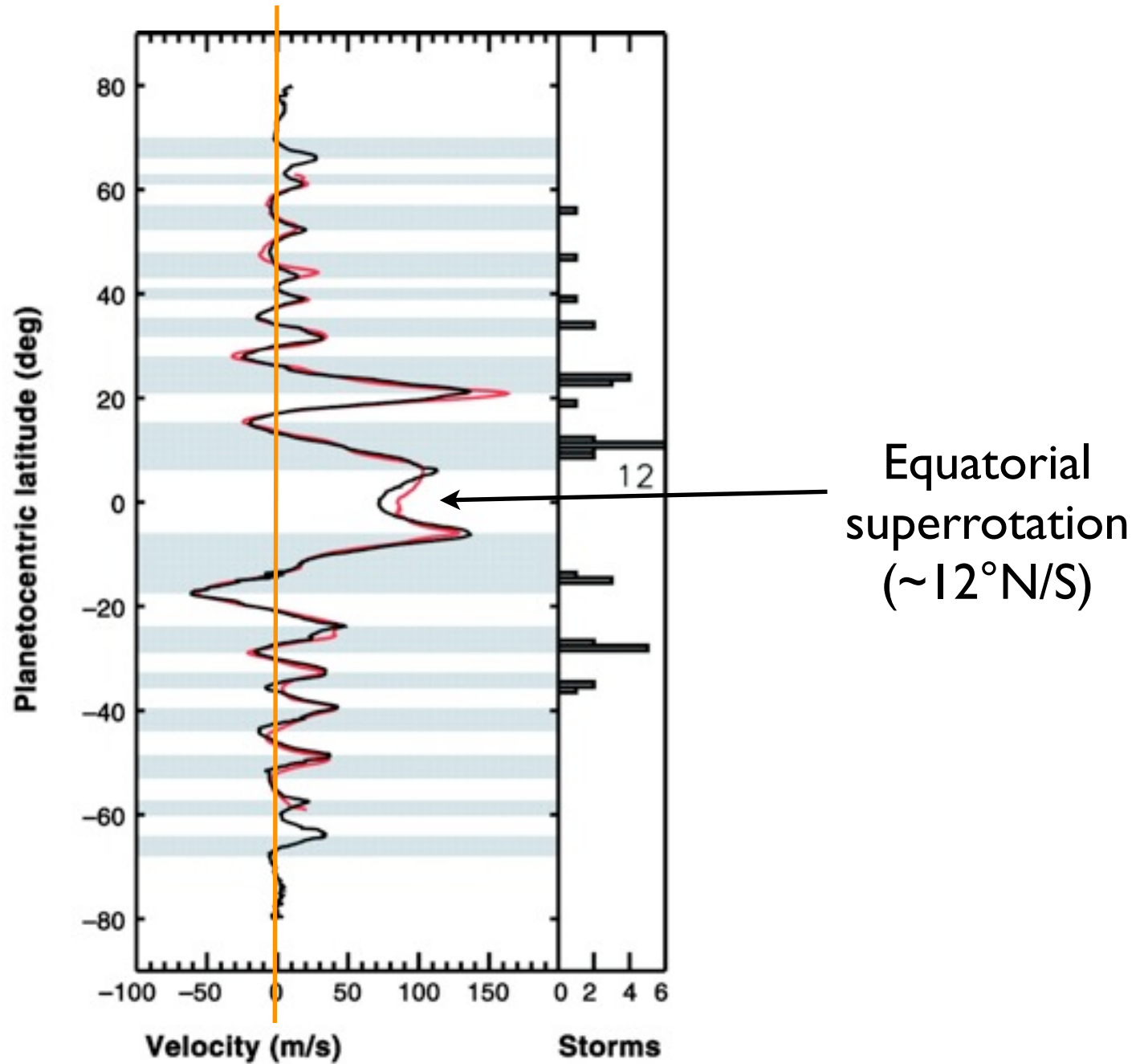
Tapio Schneider and Junjun Liu
California Institute of Technology

Jupiter zonal wind



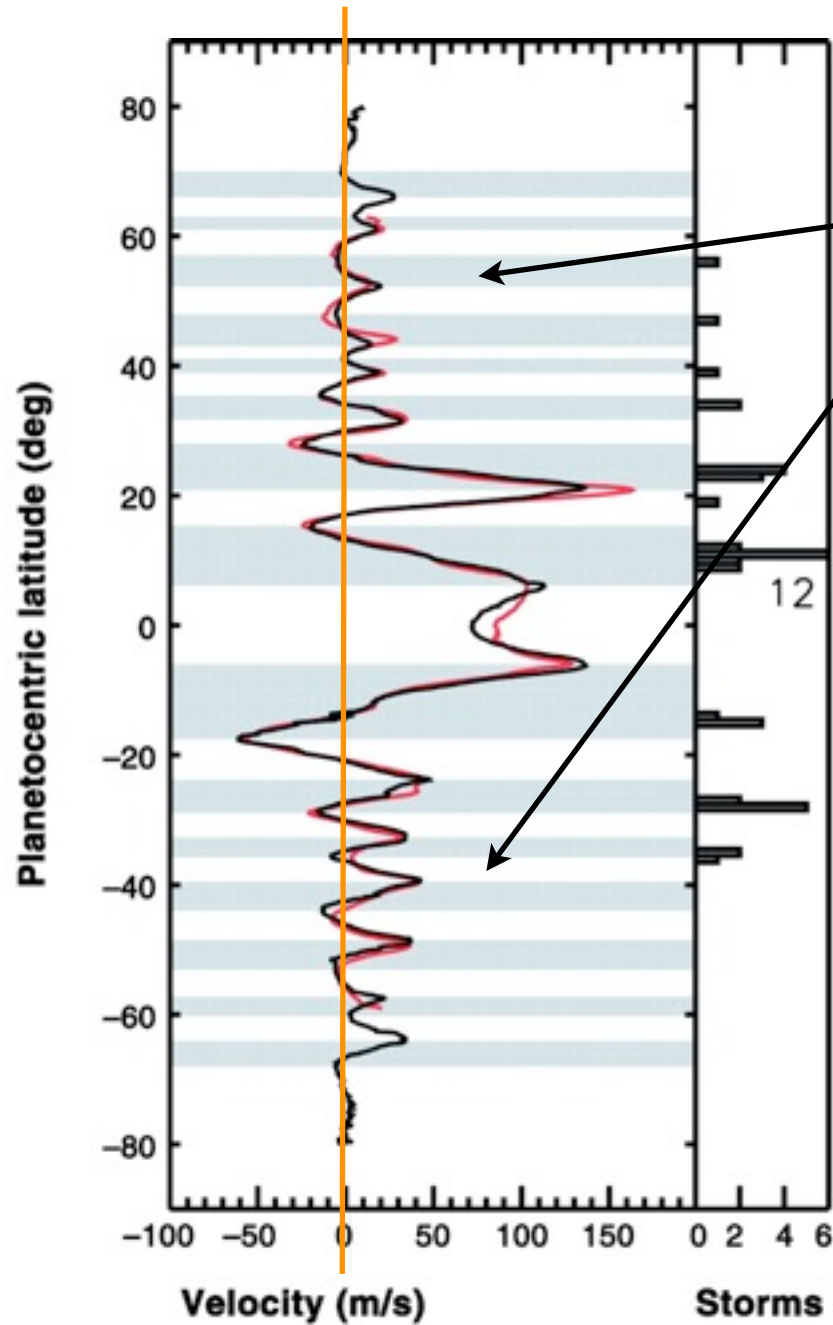
(Porco et al. 2003)

Jupiter zonal wind



(Porco et al. 2003)

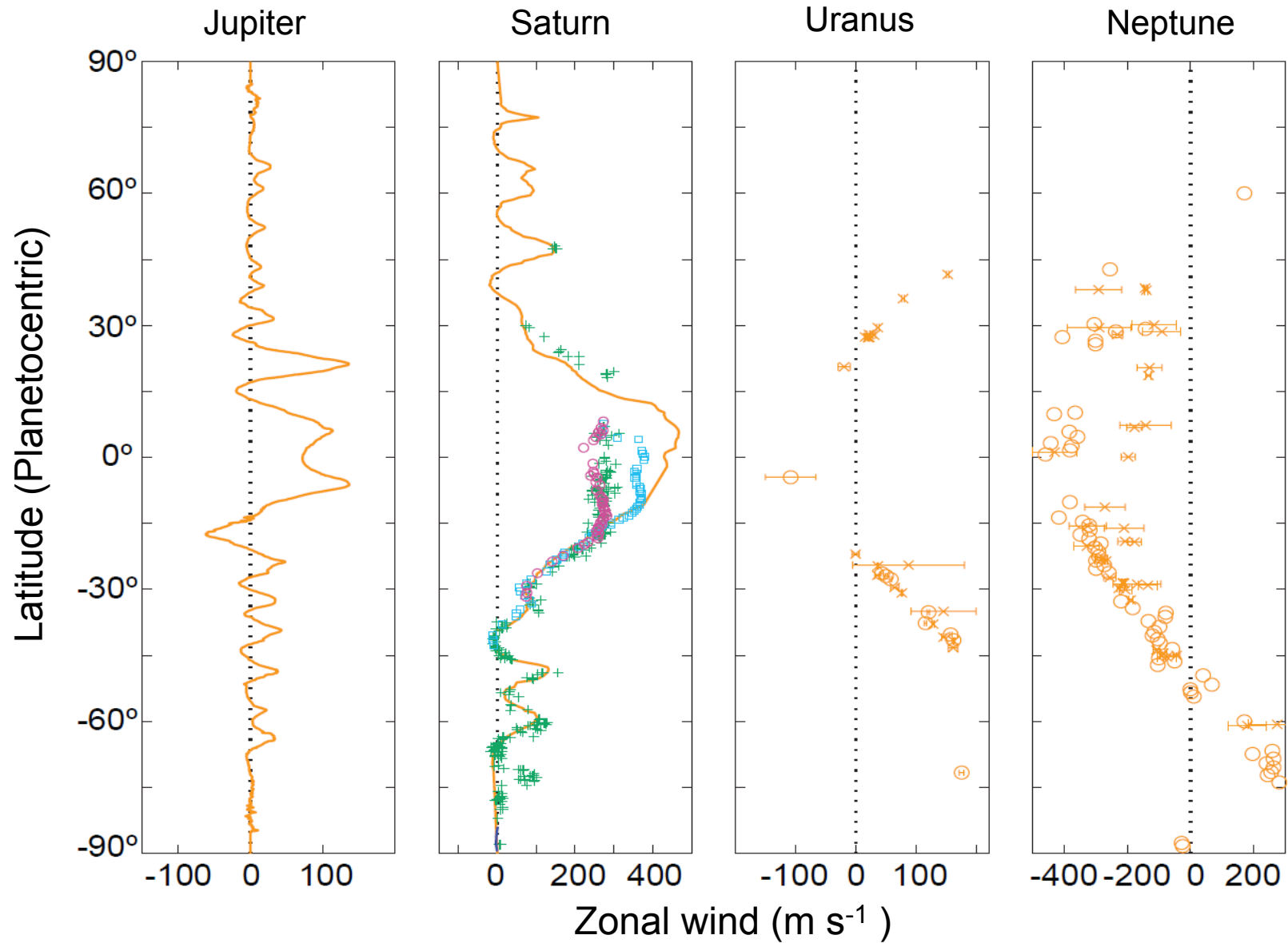
Jupiter zonal wind



Extratropical jets
($\sim 8^\circ$ spacing)

(Porco et al. 2003)

Zonal wind on all giant planets



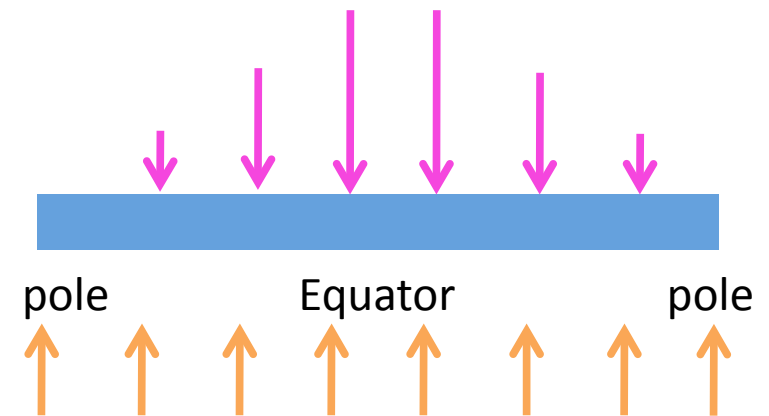
(Porco et al. 2003; Sanchez-Lavega et al. 2001; Hammel et al. 2001; Sromovsky et al. 2001)

Energy budget of giant planets

- Emit more energy than they receive from the sun
- **Internal heat flux** can generate convection
- **Differential solar radiative heating** from above

	Absorbed insolation	Internal heat flux
<i>Jupiter</i>	8.1 Wm^{-2}	5.7 Wm^{-2}
<i>Saturn</i>	2.7 Wm^{-2}	2.0 Wm^{-2}
<i>Uranus</i>	0.7 Wm^{-2}	0.04 Wm^{-2}
<i>Neptune</i>	0.3 Wm^{-2}	0.4 Wm^{-2}

(Guillot 2005)

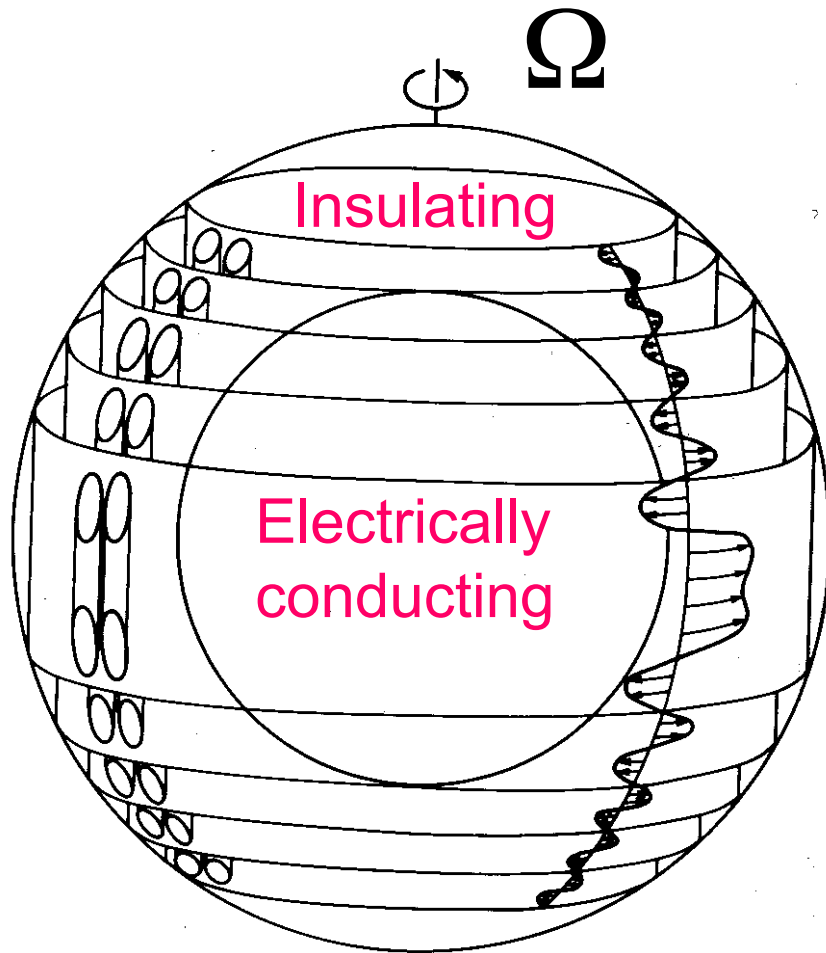


Giant planet properties

- Have similar radii and rotation rates
- Differ in energy budgets
- Very different flows:
 - Jupiter, Saturn superrotating
 - Uranus, Neptune subrotating

Differences in flows likely caused by differences in energy budgets

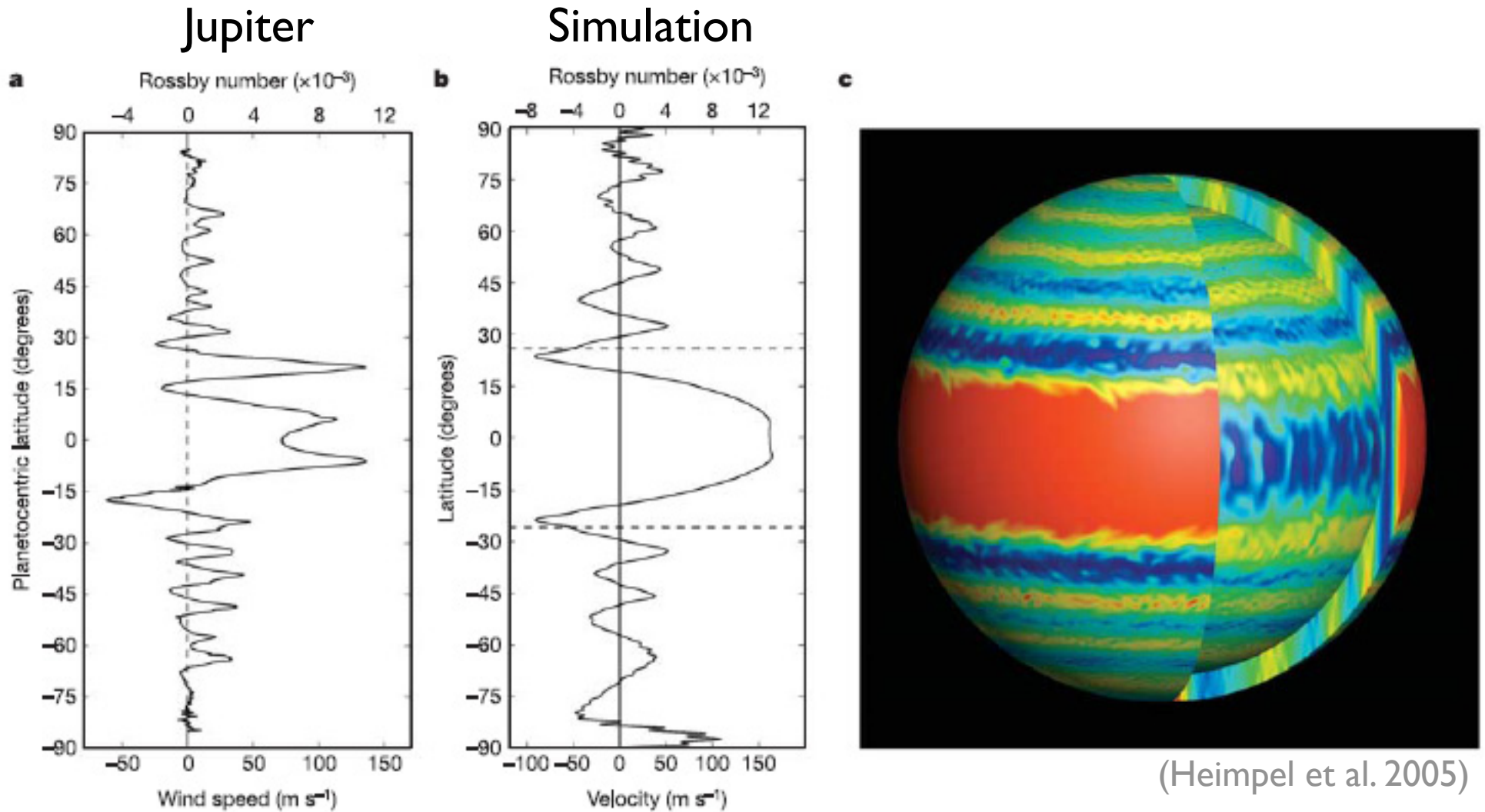
Deep-flow models



(Busse, 1983)

- Rotating Rayleigh-Benard convection
- Surface zonal winds extend along cylinders through insulating layer (Busse 1976)
- But strength of deep winds constrained by Ohmic dissipation (Liu et al. 2008)

Zonal wind in deep-flow model

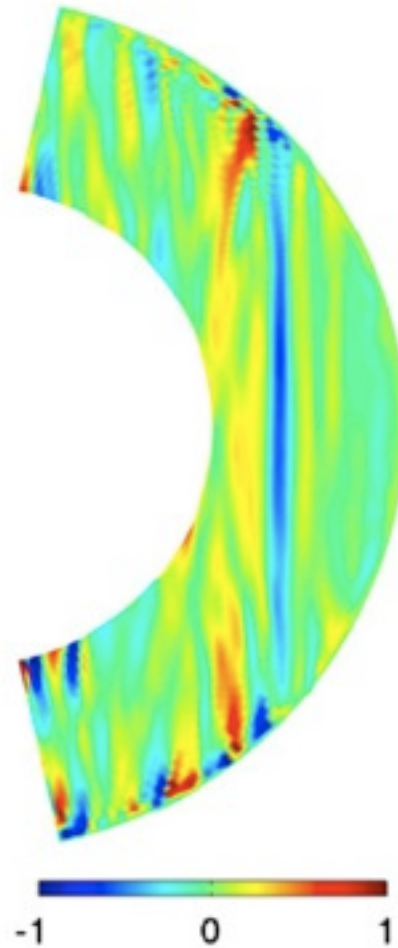


(Heimpel et al. 2005)

Implies excessive heat flux (viscous dissipation) and are ruled out by AM balance

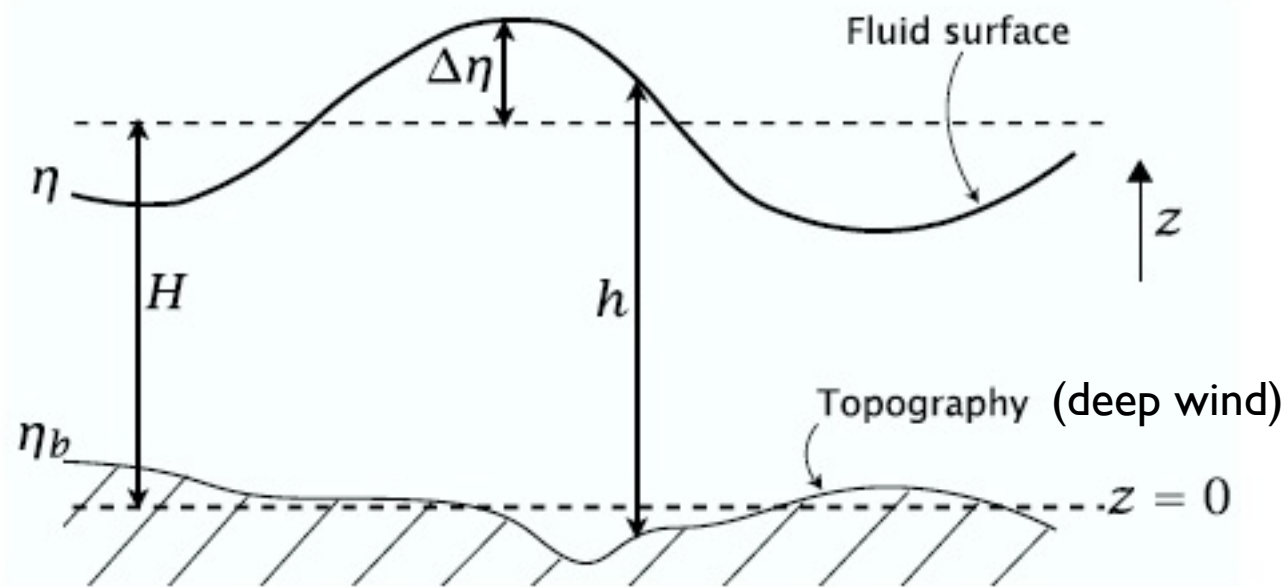
AM flux (per unit volume) is barotropic in deep-flow models

$$\nabla \cdot (\tilde{\rho} \mathbf{u}' \mathbf{u}')$$



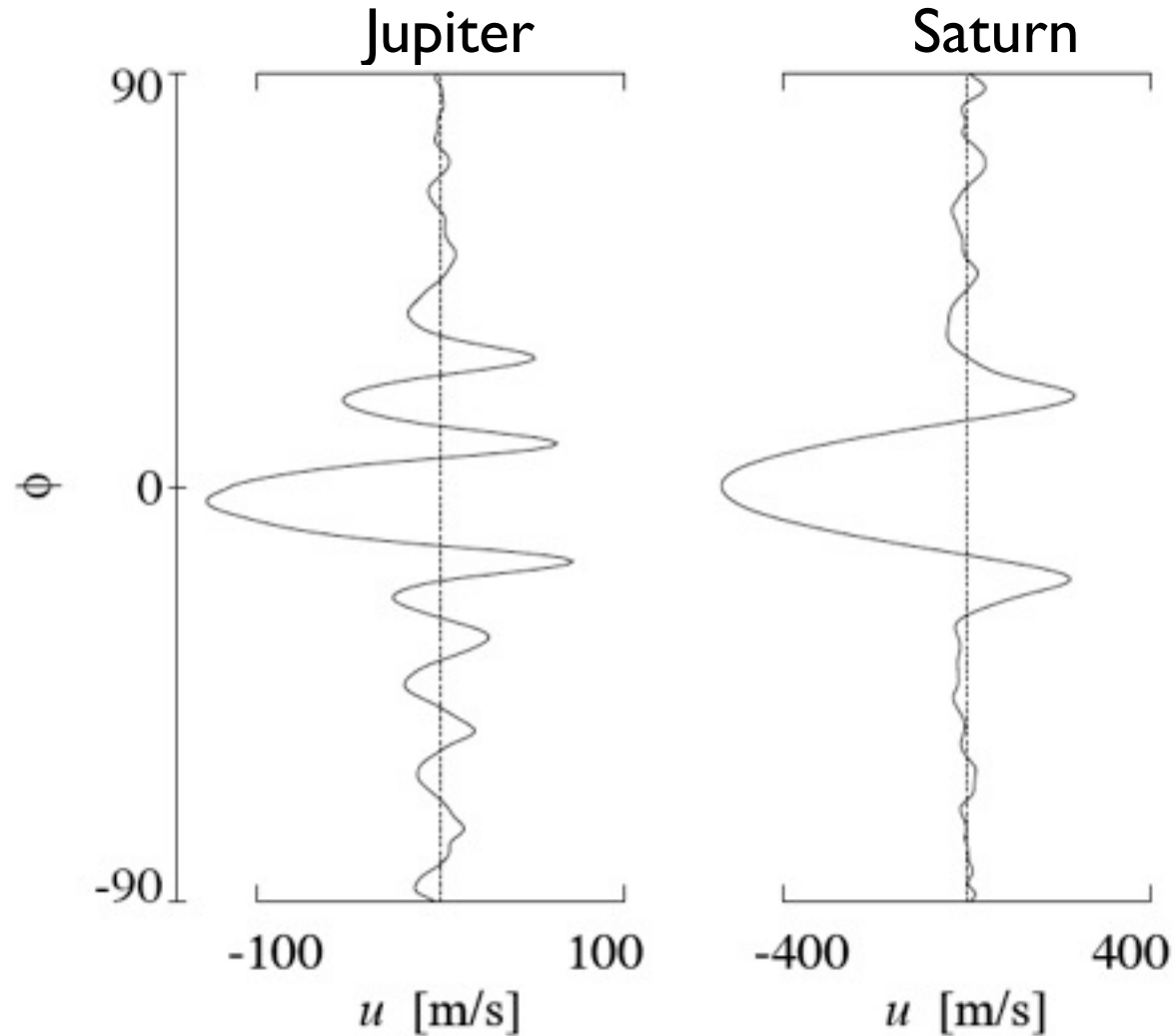
(Kaspi et al. 2009)

Shallow-flow models



- Shallow-water layer on rotating sphere
- Driven by small-scale forcing (convection) or large-scale mass/volume source (insolation gradient)
- Generation of extratropical jets by inverse cascade

Zonal wind in shallow model



- Usually does not reproduce equatorial superrotation
- Ignores baroclinicity/stratification

(Scott and Polvani 2007)

Hide's theorem and superrotation

If there is any (radial) viscous dissipation of angular momentum,

$$\frac{DM}{Dt} = \frac{\partial}{\partial r} \nu \frac{\partial M}{\partial r},$$

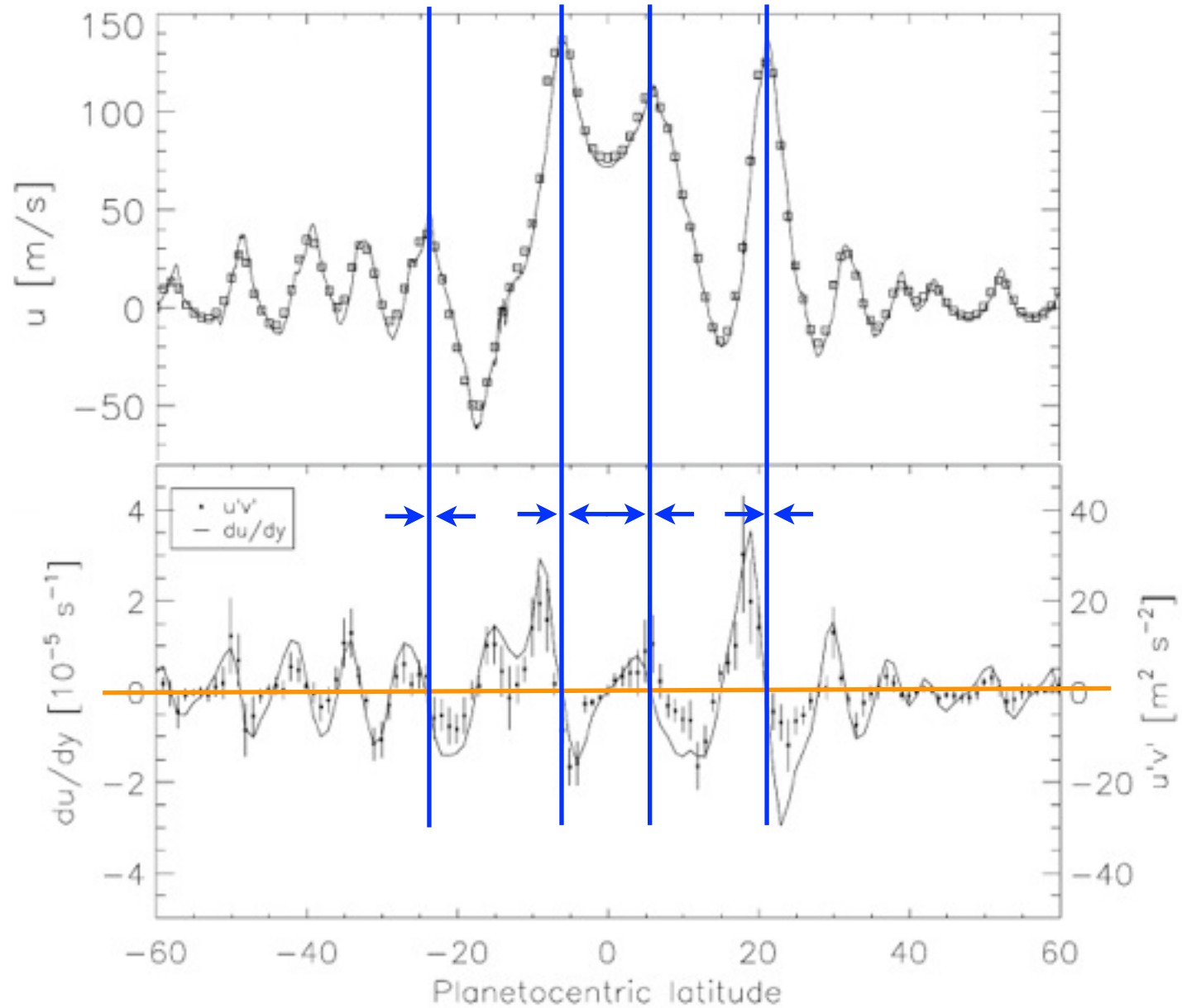
with $M = (a\Omega \cos \phi + u)a \cos \phi$, interior extrema of angular momentum are impossible in steady flow.



Therefore, $u \leq \Omega a \sin^2 \phi / \cos \phi$.

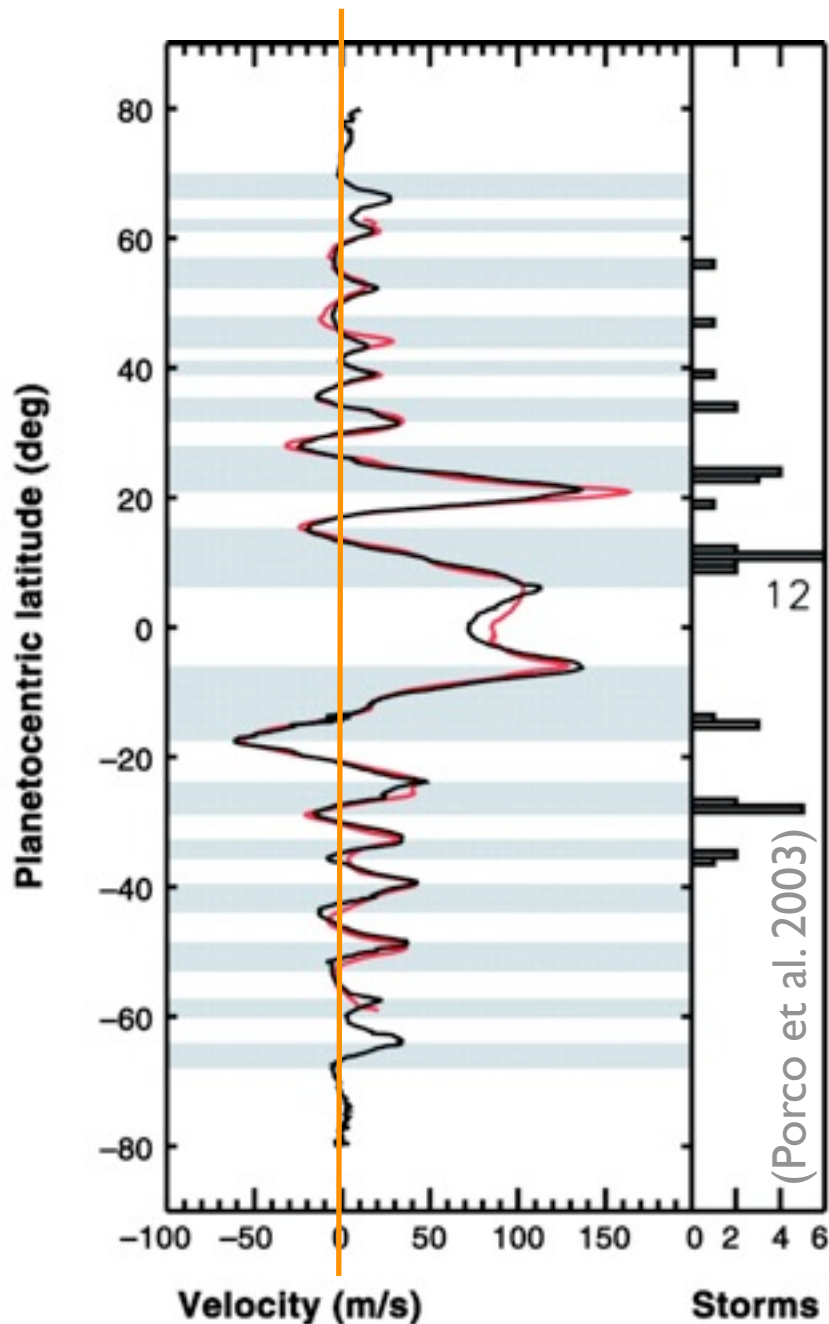
(Hide 1969; Schneider 1977)

Eddy angular momentum flux on Jupiter



(Salyk et al. 2006)

Scales of waves on Jupiter



- Gravity wave speed:

$$c \approx 450 \text{ m s}^{-1}$$

(Ingersoll & Kanamori 1995)

- Midlatitude Rossby radius:

$$c/f \sim 2000 \text{ km}$$

- Equatorial Rossby radius:

$$\sqrt{c/\beta} \sim 10,000 \text{ km} \sim 8^\circ$$

Generation of equatorial waves by convection

Thermodynamic balance in equatorial region (Charney 1963):

$$\cancel{\partial_t b} + \mathbf{v} \cdot \cancel{\nabla_h b} + N^2 w = Q$$

Sufficiently strong convective heating leads to divergence:

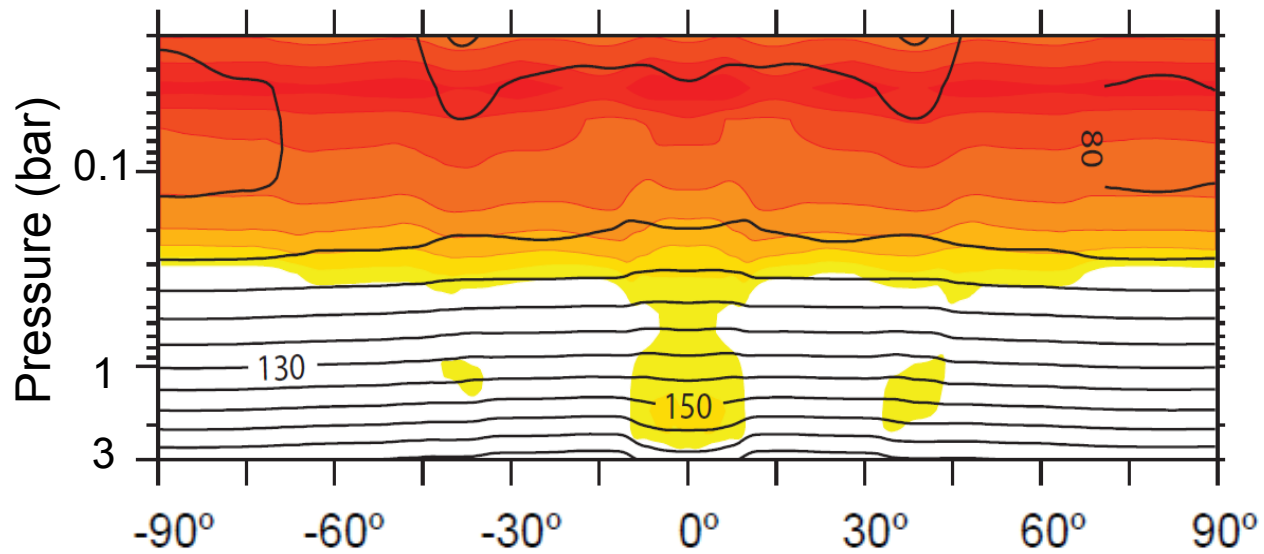
$$\nabla_h \cdot \mathbf{v}_\chi = -\partial_z w = -\partial_z(Q/N^2)$$

Divergence is source of rotational flow (Sardeshmukh & Hoskins 1988):

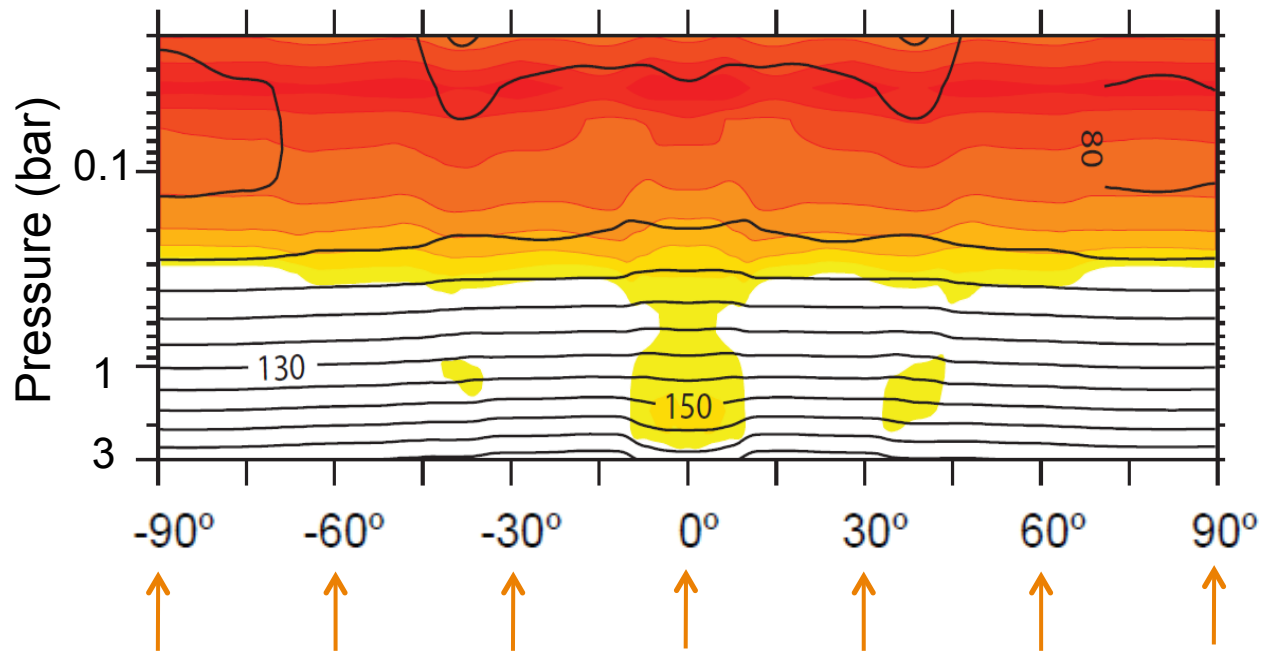
$$(\partial_t + \mathbf{v}_\Psi \cdot \nabla_h) \zeta_a = -\nabla_h \cdot (\zeta_a \mathbf{v}_\chi)$$

Convective heating at weak stratification generates Rossby waves that propagate out of equatorial waveguide

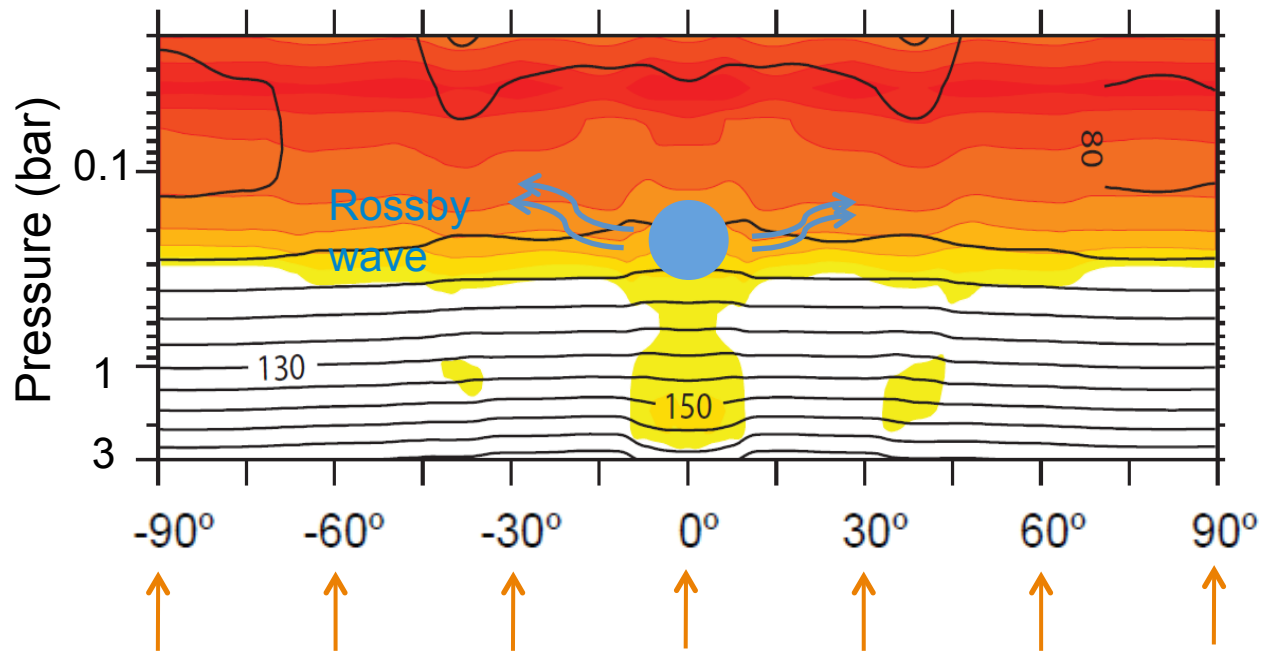
Uniform convection generates equatorial Rossby waves, which transport angular momentum toward equator



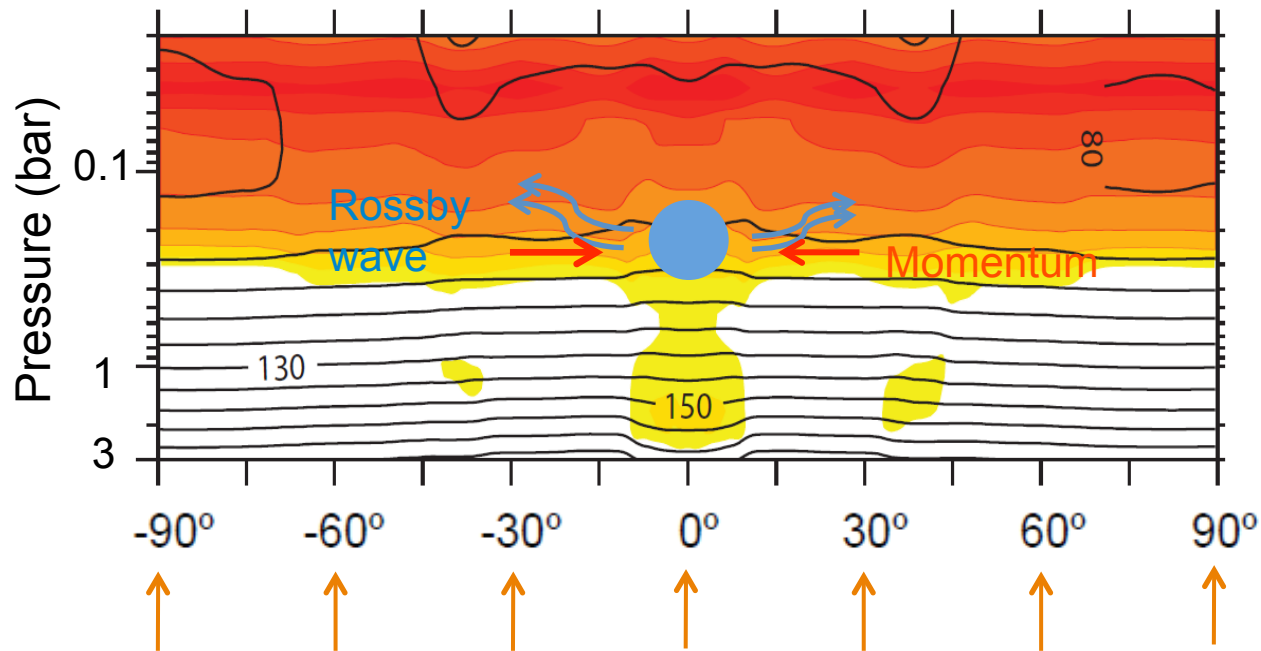
Uniform convection generates equatorial Rossby waves, which transport angular momentum toward equator



Uniform convection generates equatorial Rossby waves, which transport angular momentum toward equator



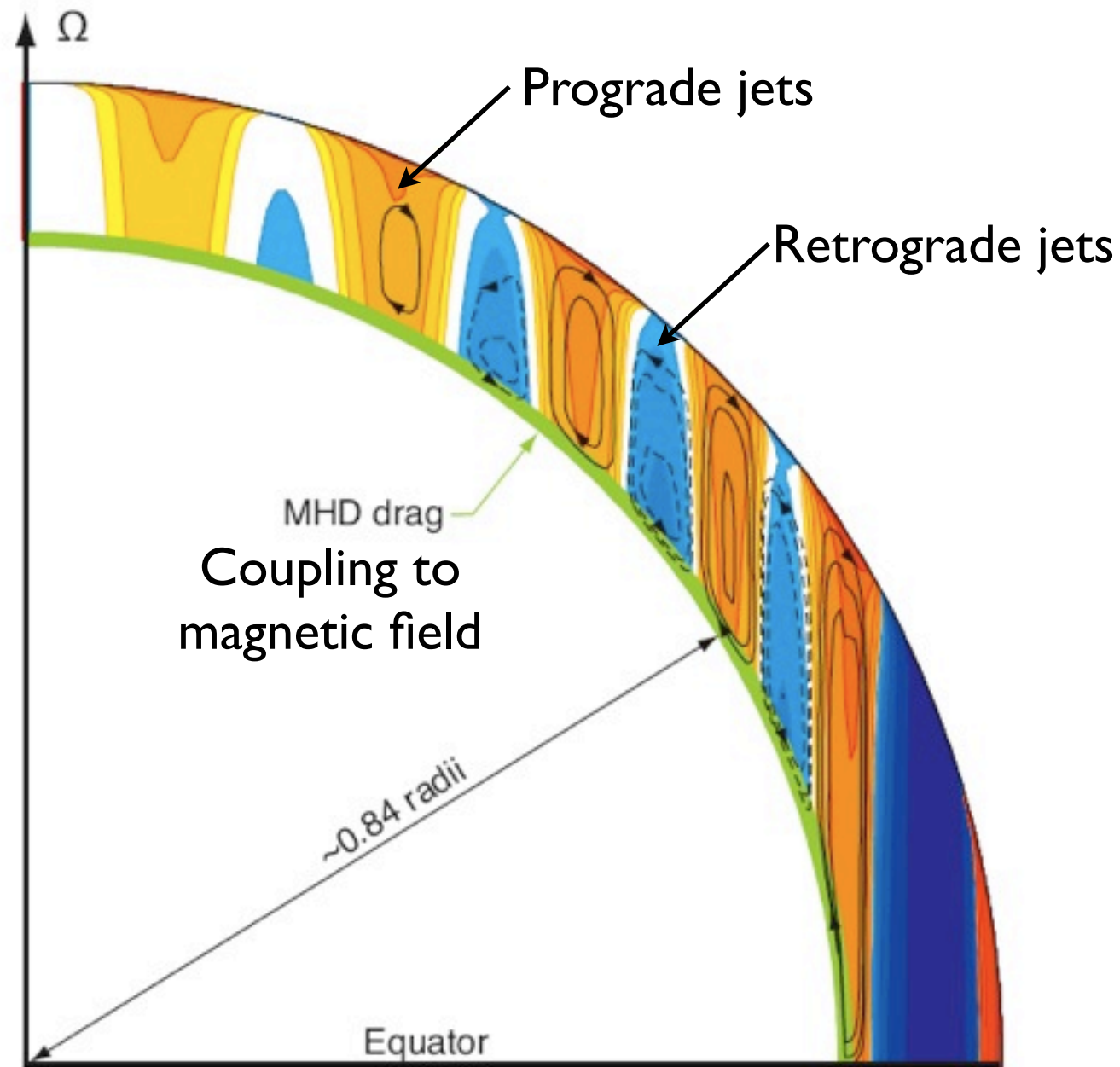
Uniform convection generates equatorial Rossby waves, which transport angular momentum toward equator



Giant planet GCM

- Ideal-gas atmosphere in thin shell with Jovian rotation rate, gravitational acceleration, gas constant, etc.
- Scattering gray radiative transfer with diffuse insolation
- Quasi-equilibrium dry convection scheme
- Exponential SGS filter in horizontal
- Up to T213 horizontal resolution, 30 vertical levels
- Imposed *uniform* heat flux at lower boundary
- Rayleigh drag at artificial lower boundary at 3 bar

Mean meridional circulations on Jupiter

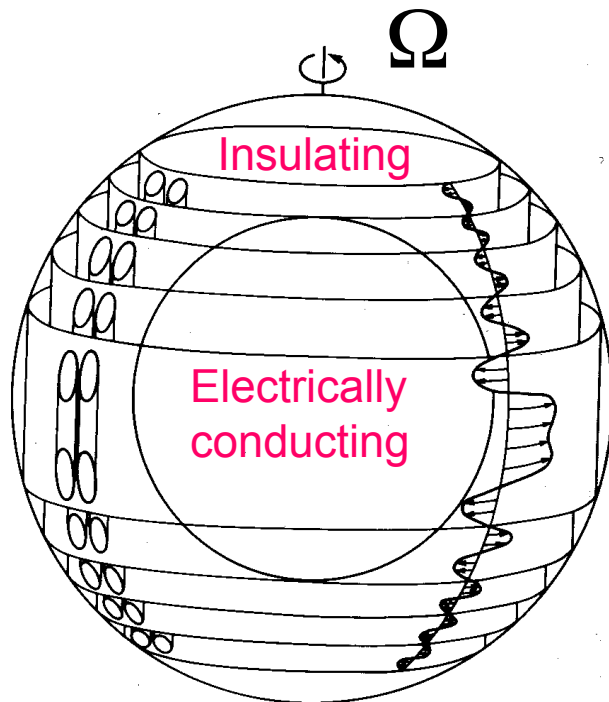


(Schneider & Liu 2009)

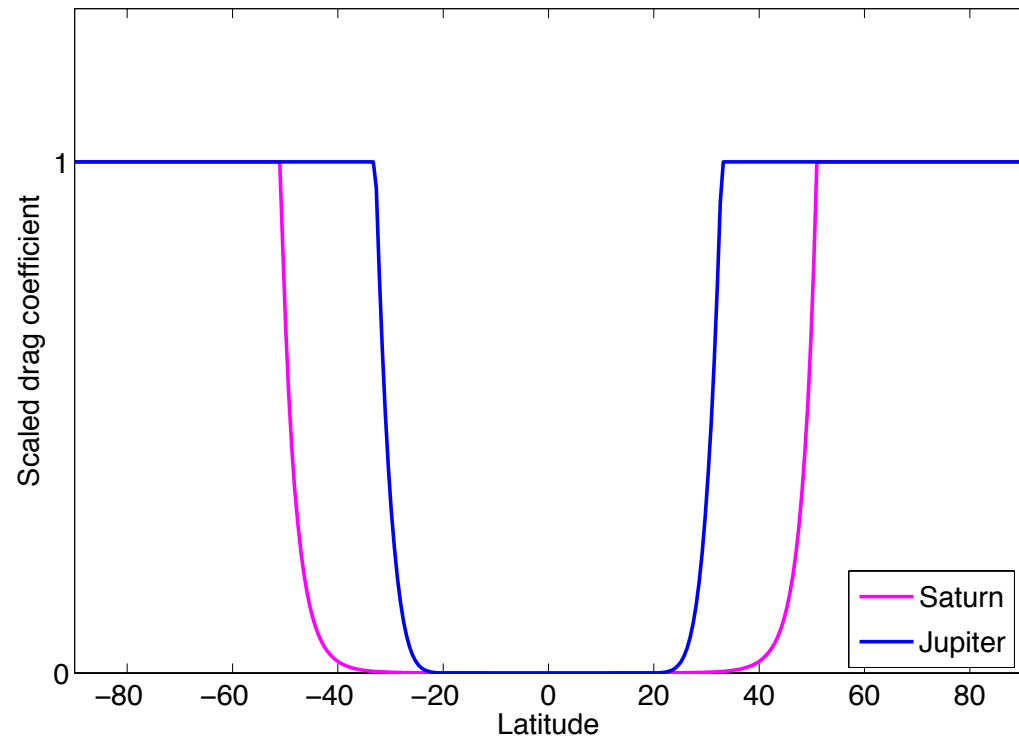
Modeling of deep MHD drag in thin shell

Model momentum dissipation as Rayleigh drag

$$\partial_t \mathbf{v} \dots = -r \mathbf{v}$$

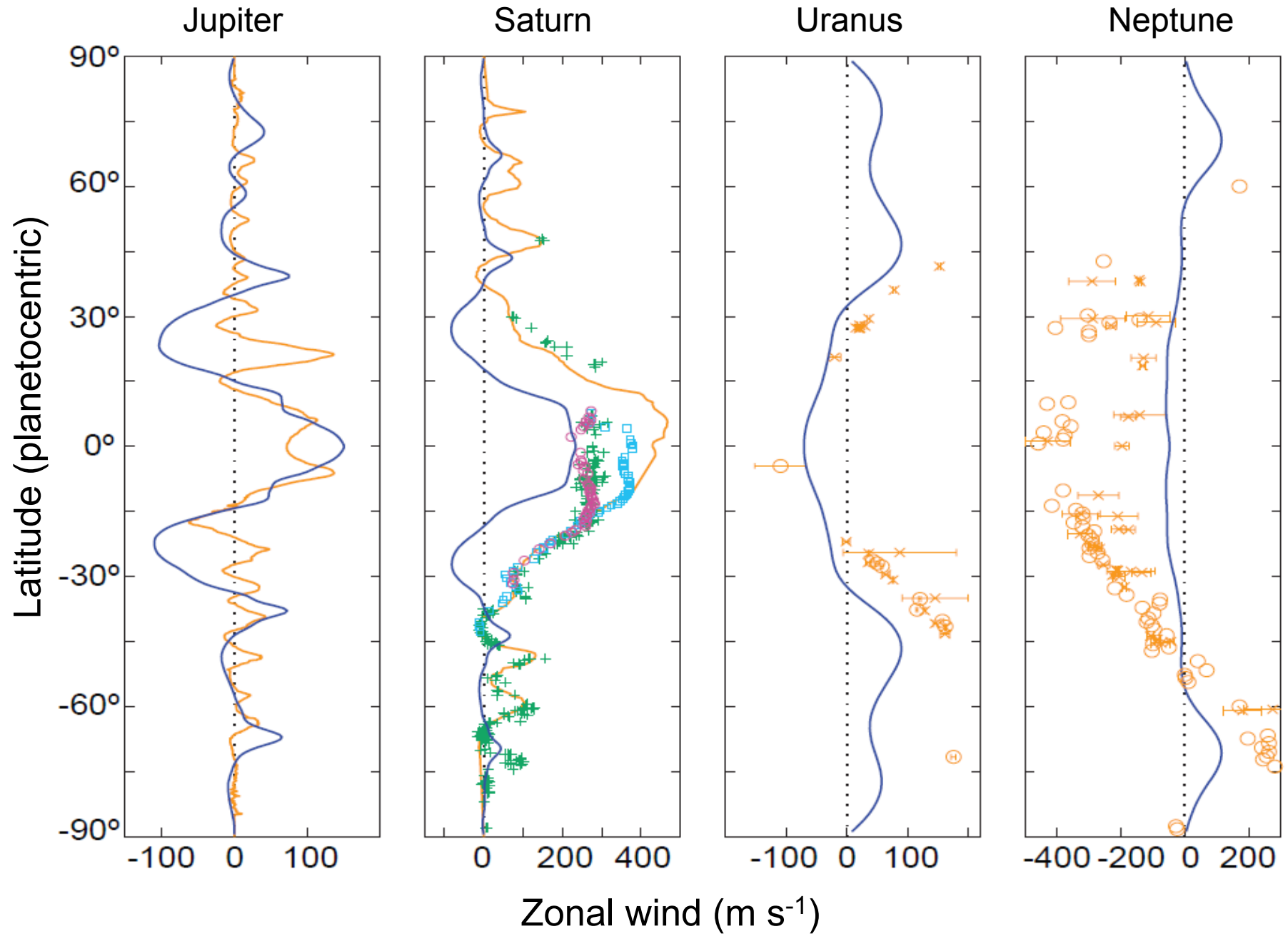


(Busse, 1983)



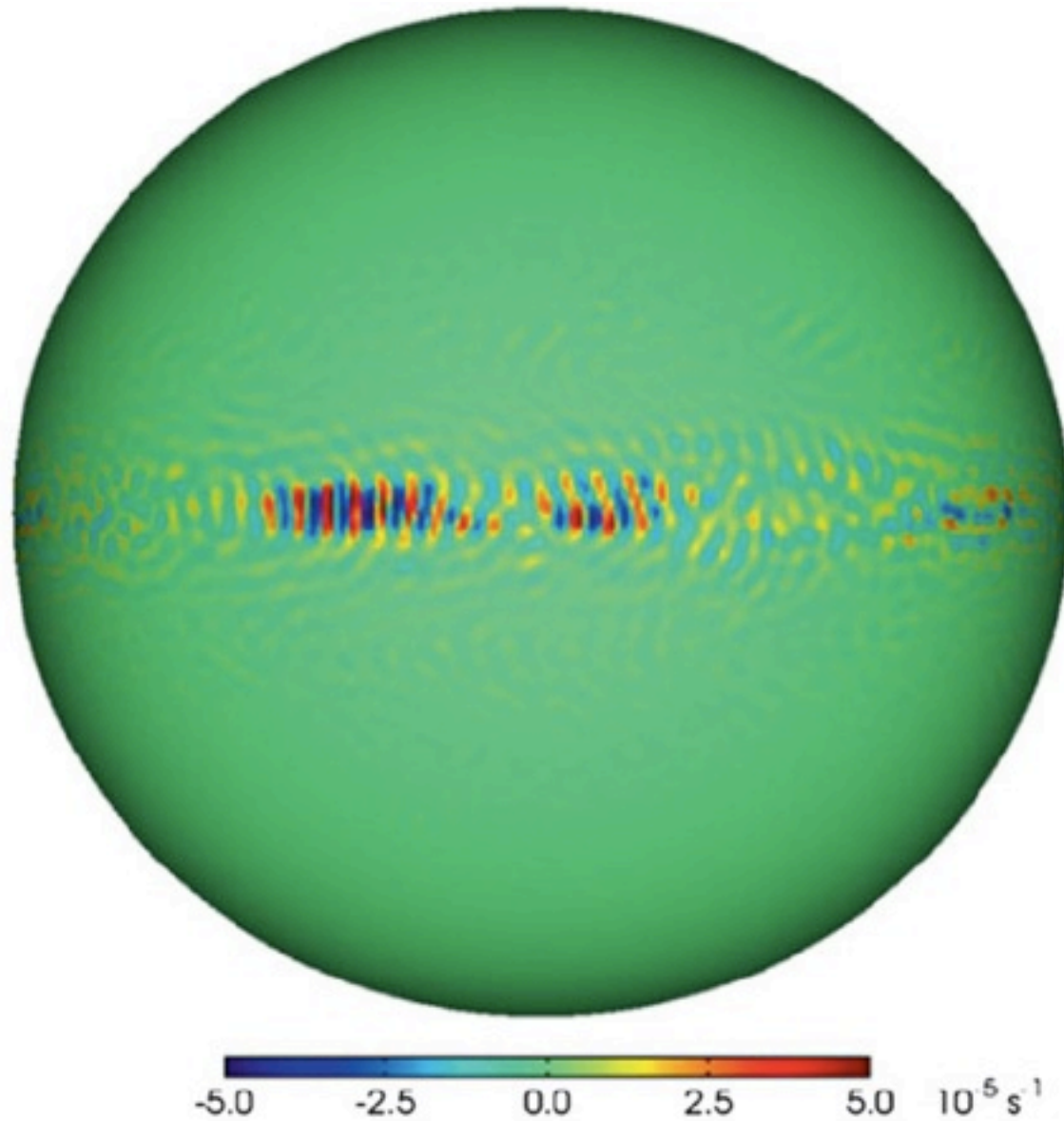
(Liu et al. 2008)

Simulated zonal wind in upper troposphere



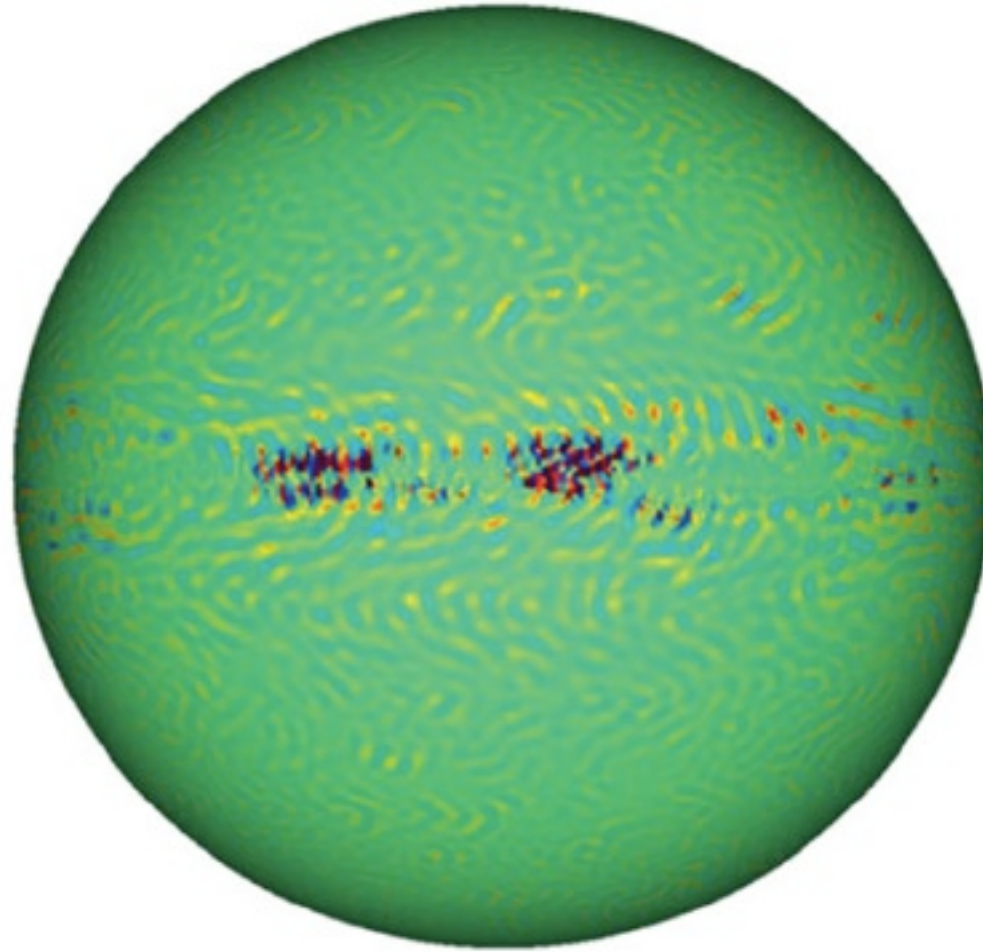
(Liu & Schneider 2009)

Divergence (Jupiter upper troposphere)



(Schneider & Liu 2009)

Rossby wave source (Jupiter troposphere)

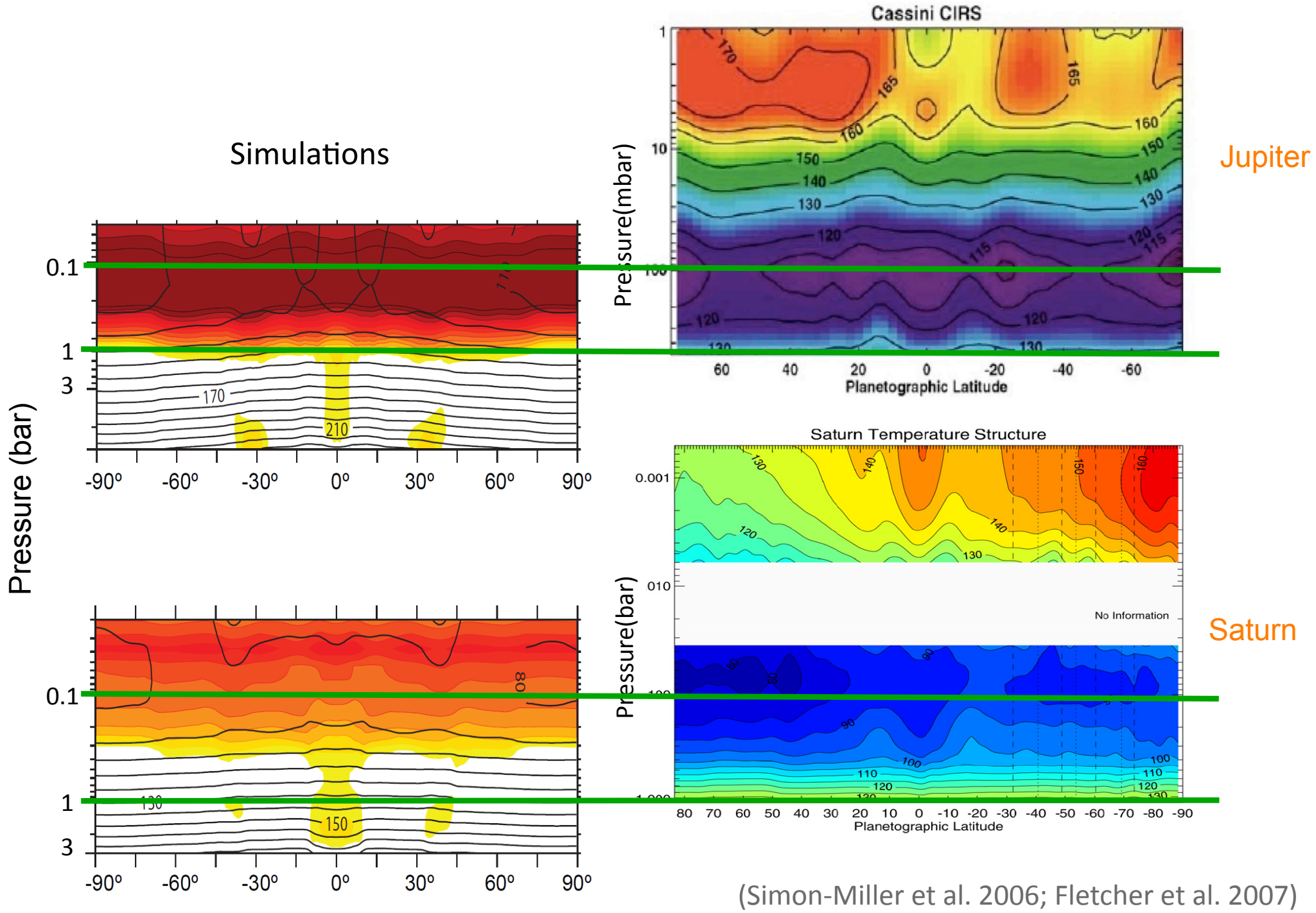


-1.0 -0.5 0.0 0.5 1.0 10^9 s^{-2}

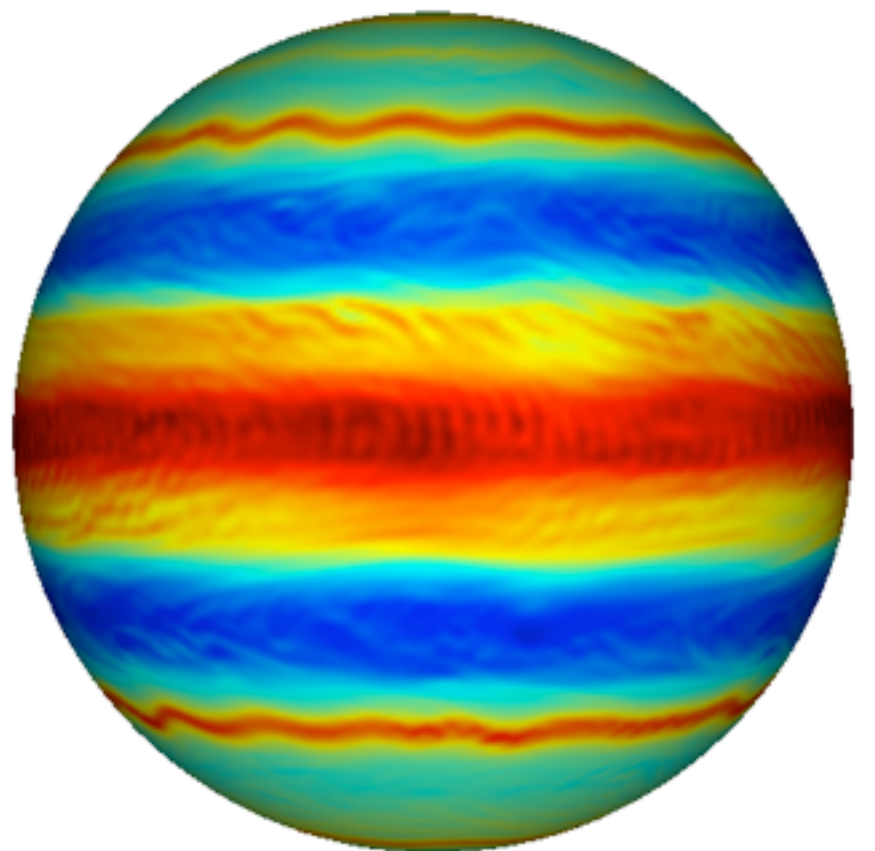
$$R = -\nabla_h \cdot (\zeta_a \mathbf{v}_\chi - \overline{\zeta_a \mathbf{v}_\chi})$$

(Schneider & Liu 2009)

Temperature: Comparison with observations



Zonal velocity in Jupiter simulation (100 Earth days)

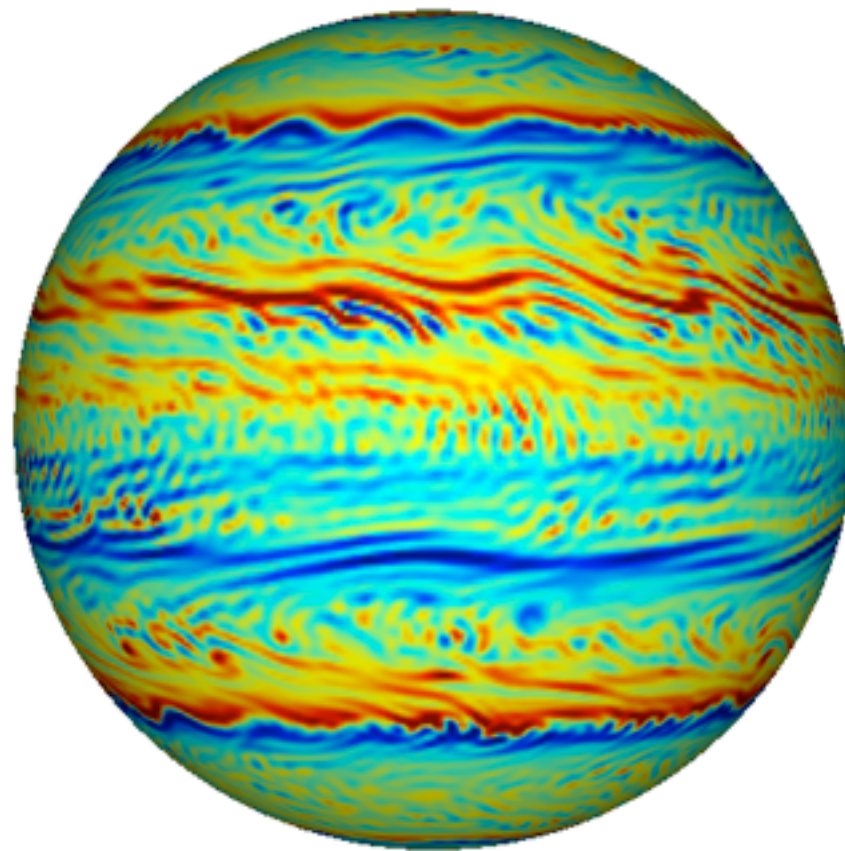


-160 -80 0 80 160 m s^{-1}

retrograde

prograde

Vorticity in Jupiter simulation (100 Earth days)



$-4.0\text{e-}05$ $-2.0\text{e-}05$ $0.0\text{e+}00$ $2.0\text{e-}05$ $4.0\text{e-}05 \text{ s}^{-1}$

(Schneider & Liu 2009)

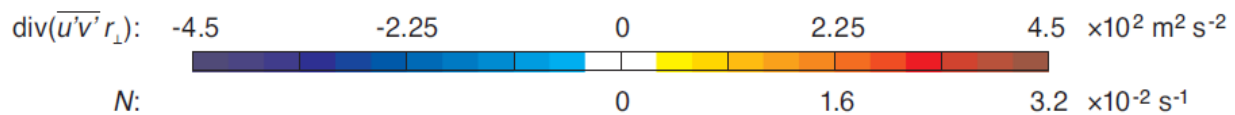
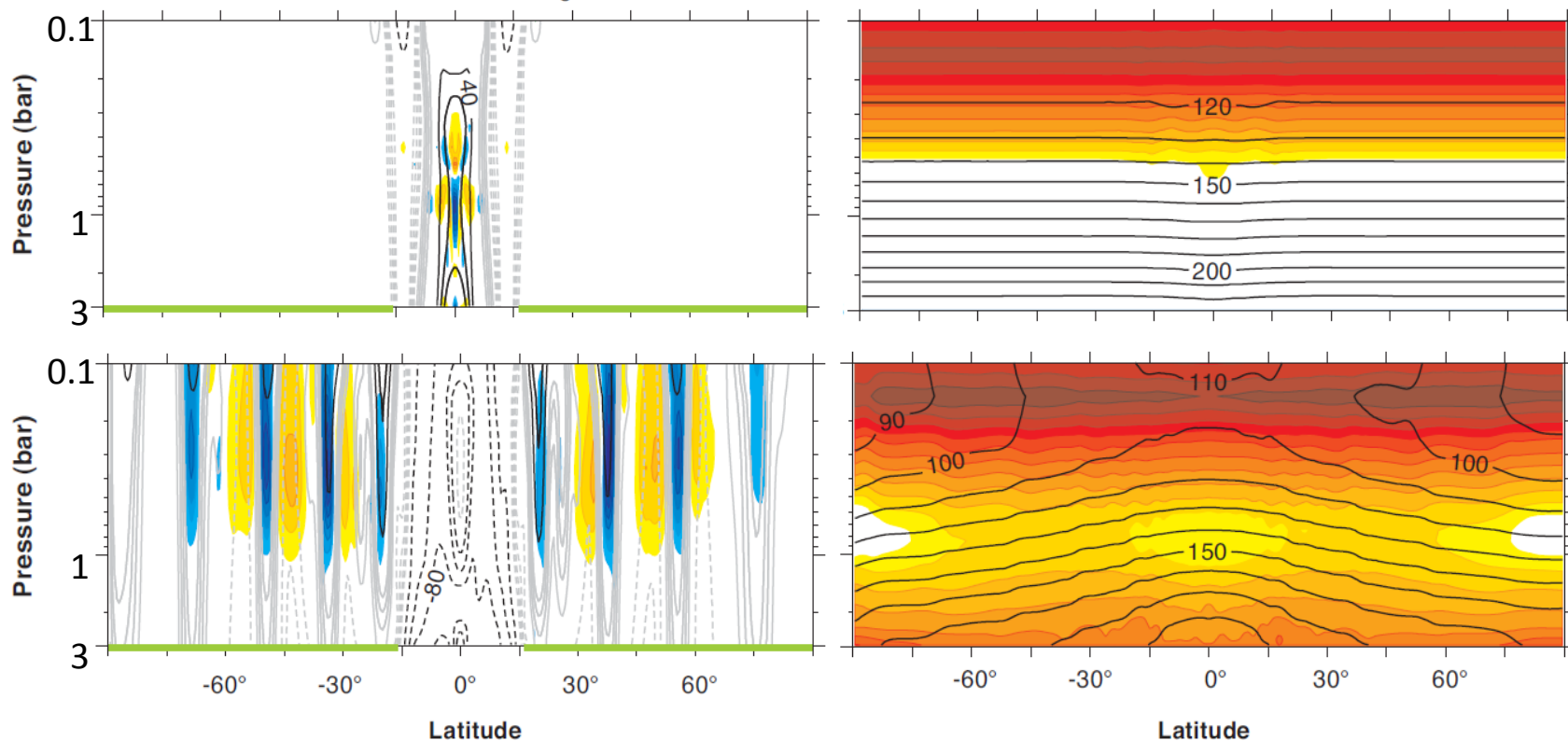
Jupiter control simulations

Uniform solar radiation

No internal heatflux

u, Eddy momentum divergence

T, N



(Schneider & Liu 2009)

Why is Saturn's equatorial jet stronger and wider than Jupiter's?

- Width of the equatorial jet is set by the equatorial Rossby radius:

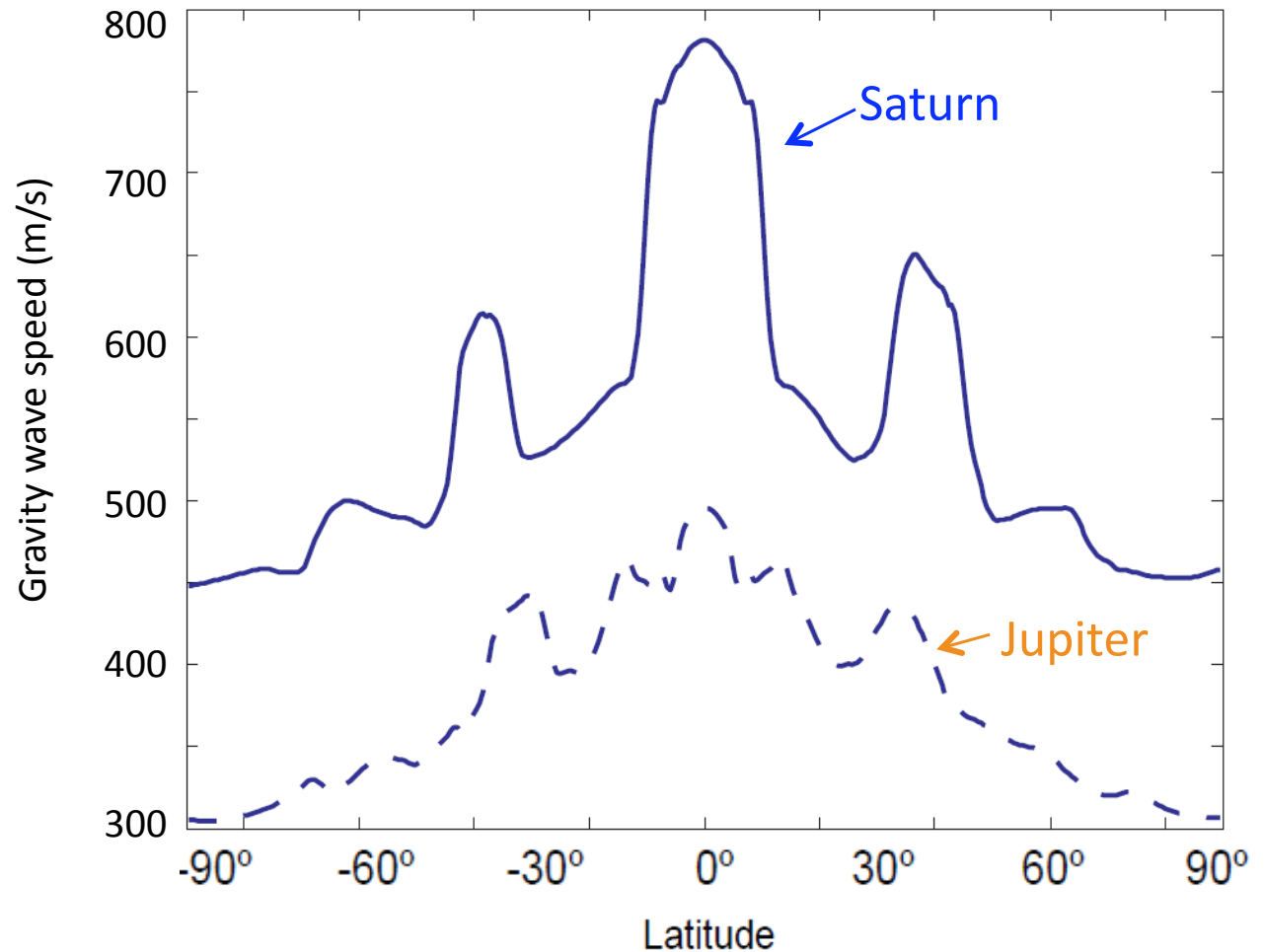
$$L = \sqrt{c/\beta}$$

$$c = \int_{p_t}^{p_s} N_p dp$$

$$N_p^2 = -(\bar{\rho}\bar{\theta})^{-1} \overline{\partial_p \theta}$$

- By vorticity mixing argument, strength of the equatorial jet increases with width:

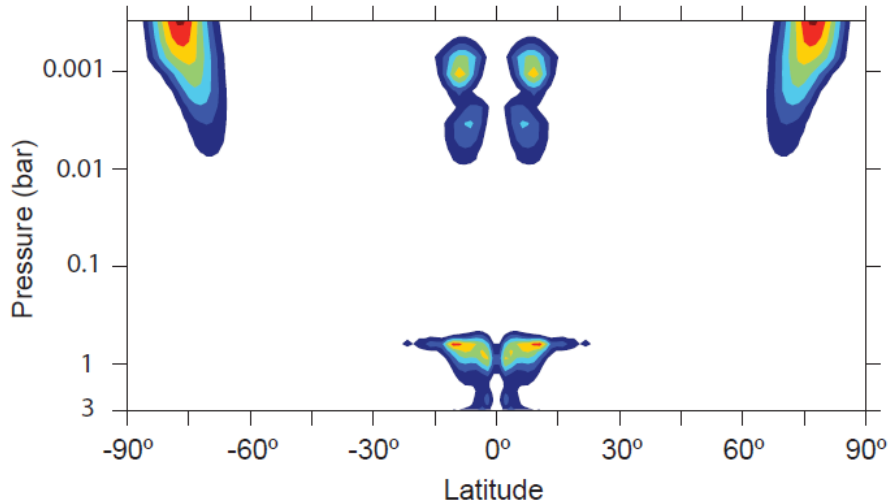
$$U \sim L^2 \beta / 2 \sim c/2$$



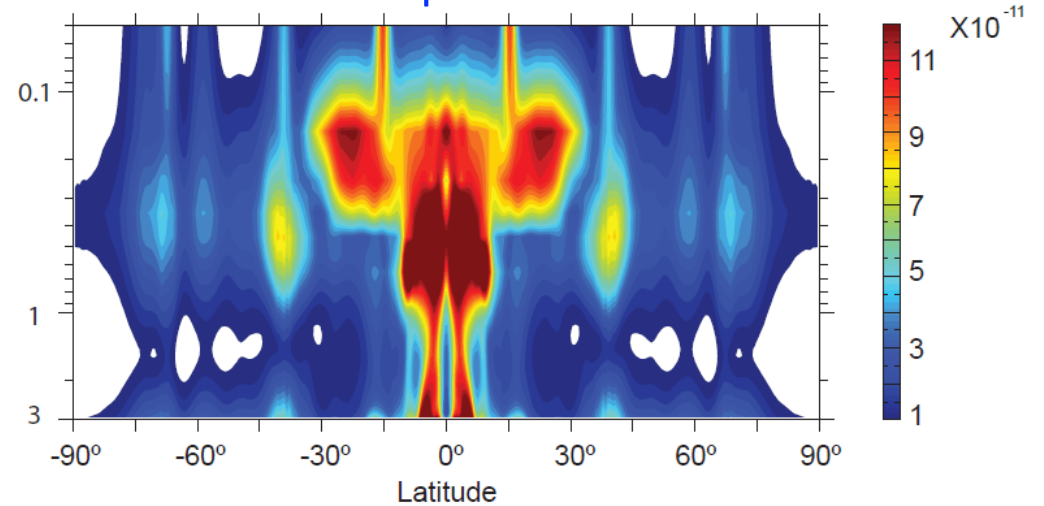
(Schneider & Liu 2009)

RMS Rossby wave source in Jupiter and Neptune simulations

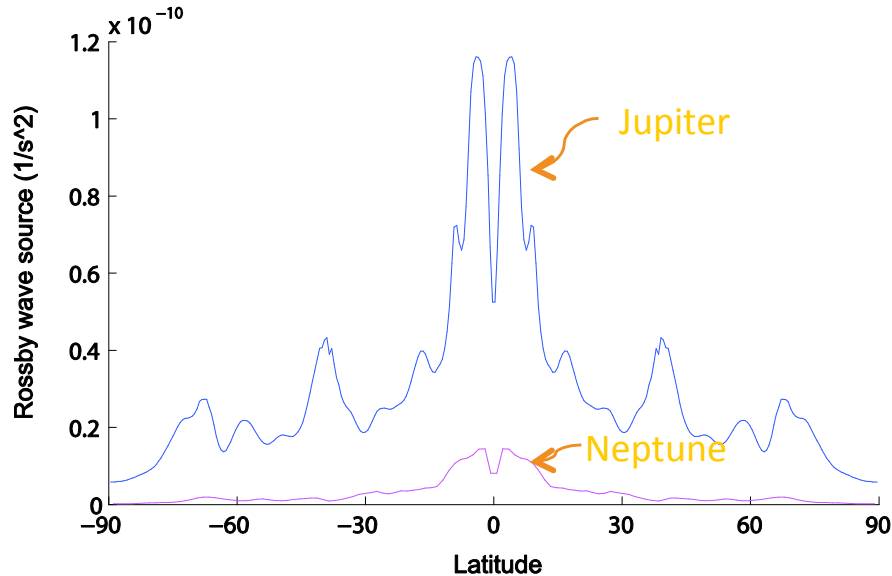
Neptune



Jupiter



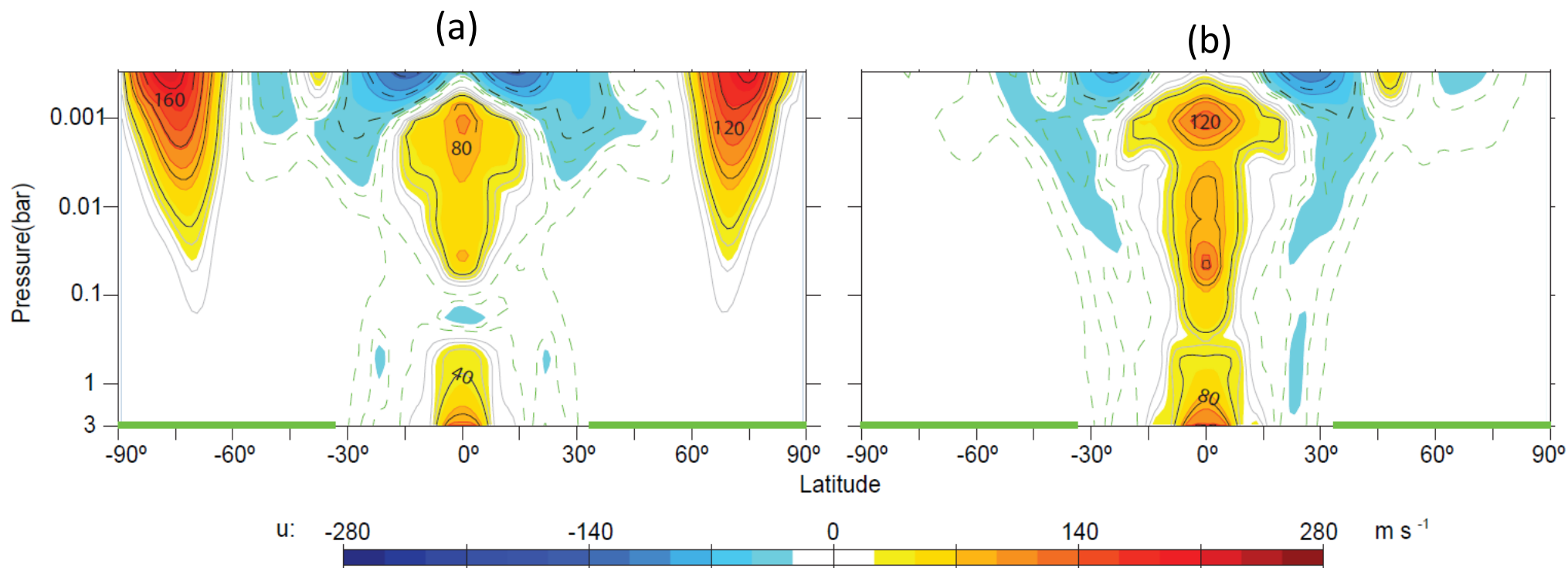
Vertically integrated Rossby wave source



- Jupiter's vertically integrated Rossby wave source is **an order of magnitude larger** than Neptune's.

(Liu & Schneider 2009)

Neptune control simulation



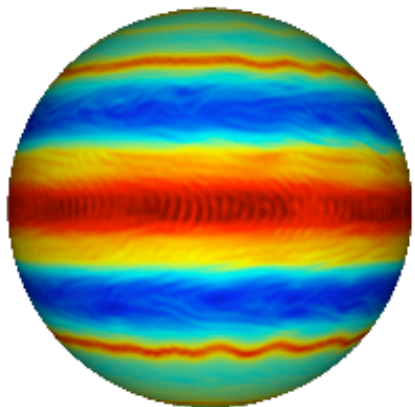
(a) Neptune's insolation and Saturn's internal heat flux 2.01 W m⁻²

(b) Uniform insolation and Neptune's internal heat flux 0.43 W m⁻²

(Liu & Schneider 2009)

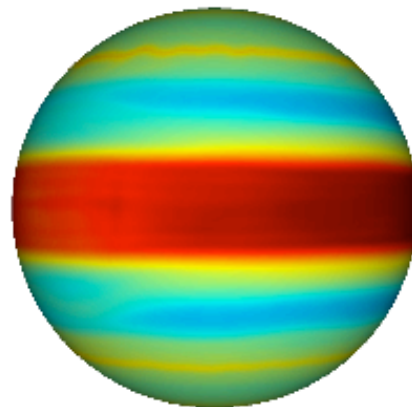
Instantaneous zonal wind and relative vorticity

Jupiter



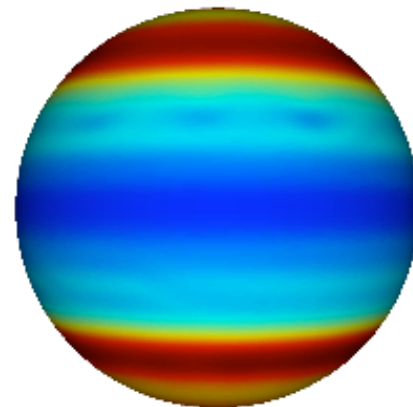
-160 -80 0 80 160 m s^{-1}

Saturn



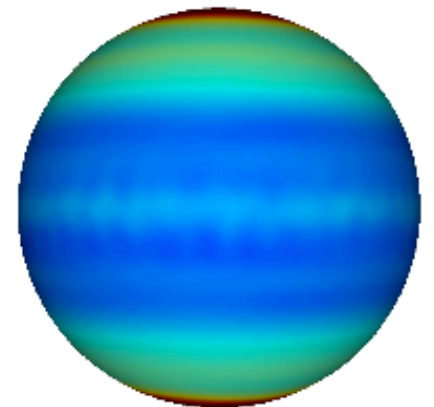
-240 -120 0 120 240 m s^{-1}

Uranus

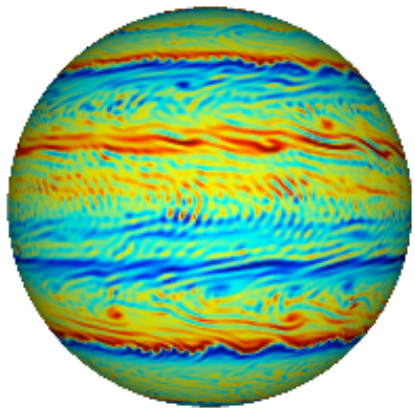


-70 -35 0 35 70 m s^{-1}

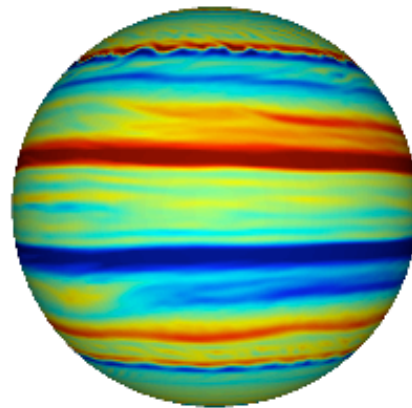
Neptune



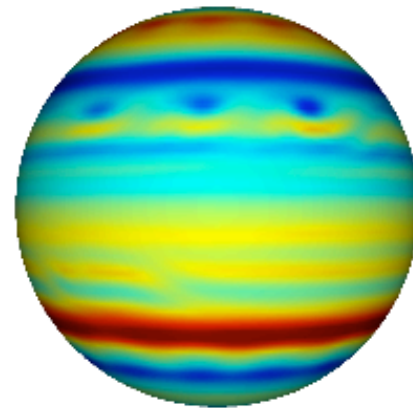
-100 -50 0 50 100 m s^{-1}



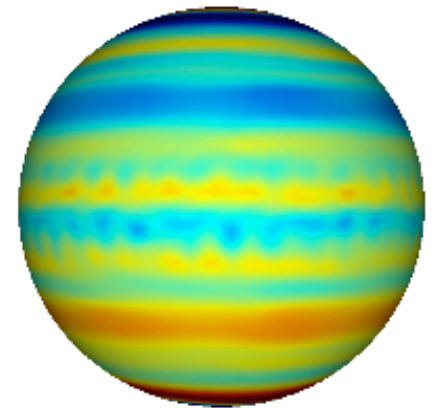
-4.0 -2.0 0.0 2.0 4.0 10^6 s^{-1}



-3.0 -1.5 0.0 1.5 3.0 10^6 s^{-1}



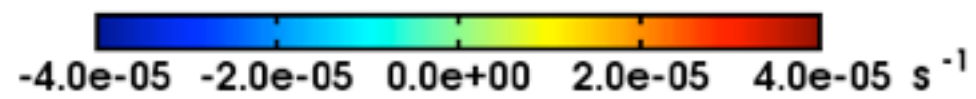
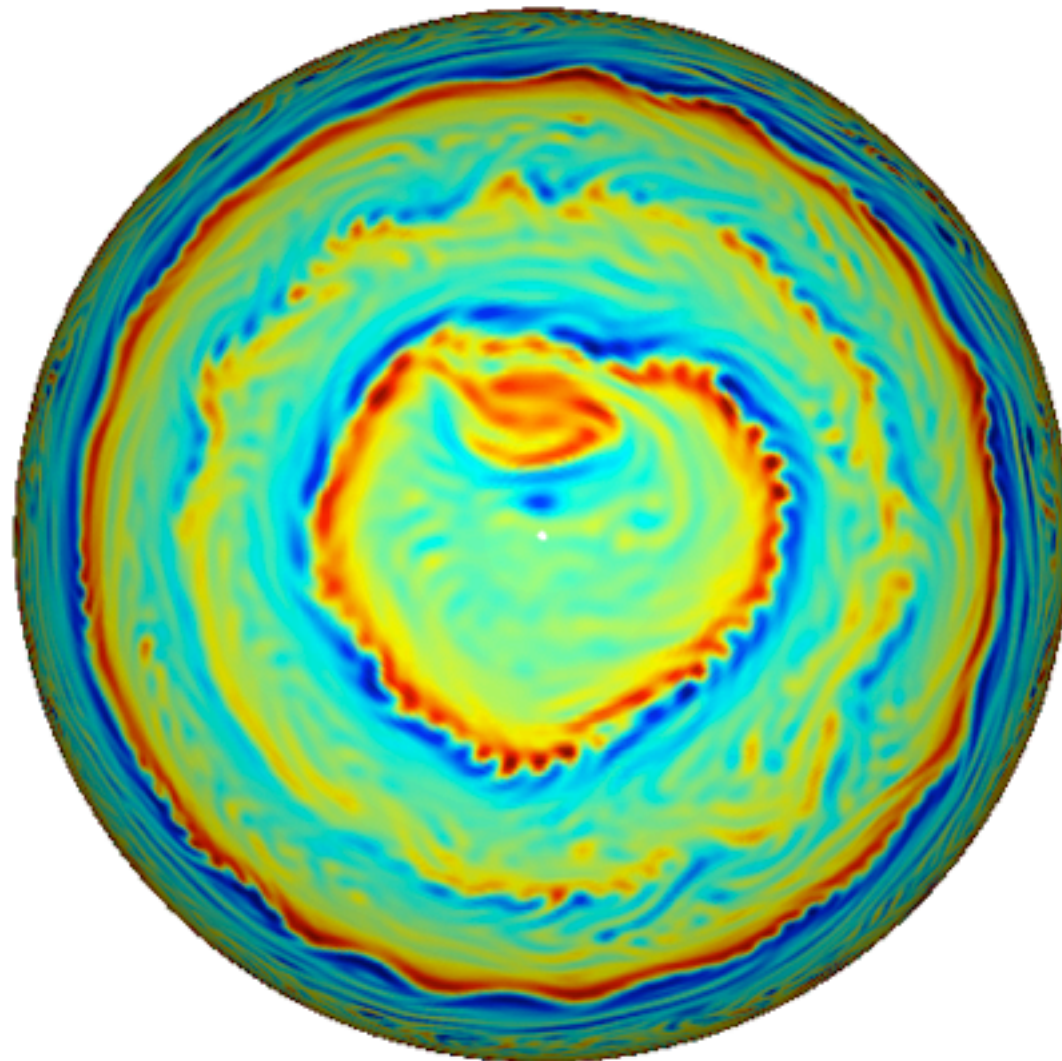
-2.0 -1.0 0.0 1.0 2.0 10^6 s^{-1}



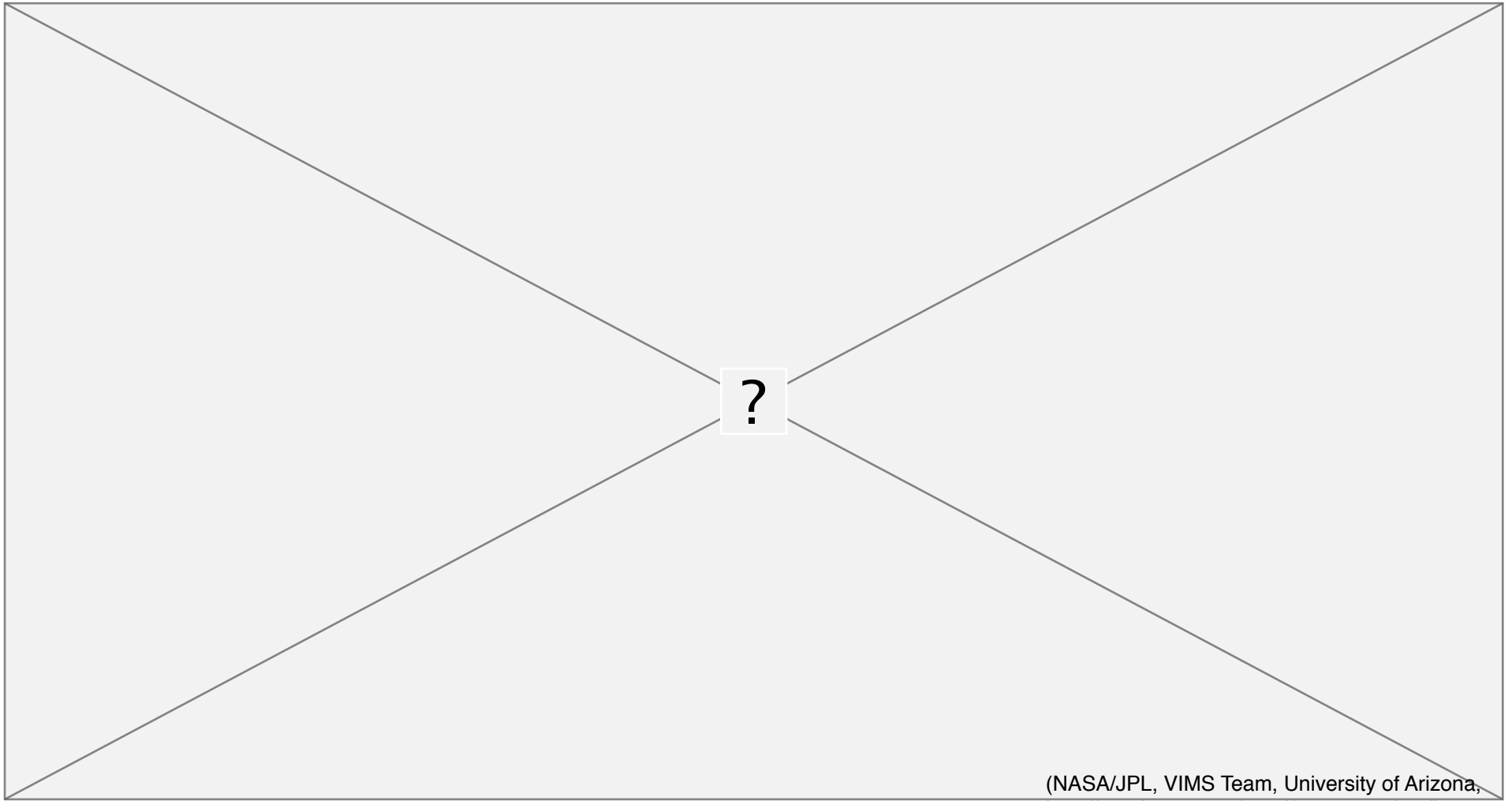
-2.0 -1.0 0.0 1.0 2.0 10^6 s^{-1}

(Liu & Schneider 2009)

Vorticity in Jupiter simulation (north pole)

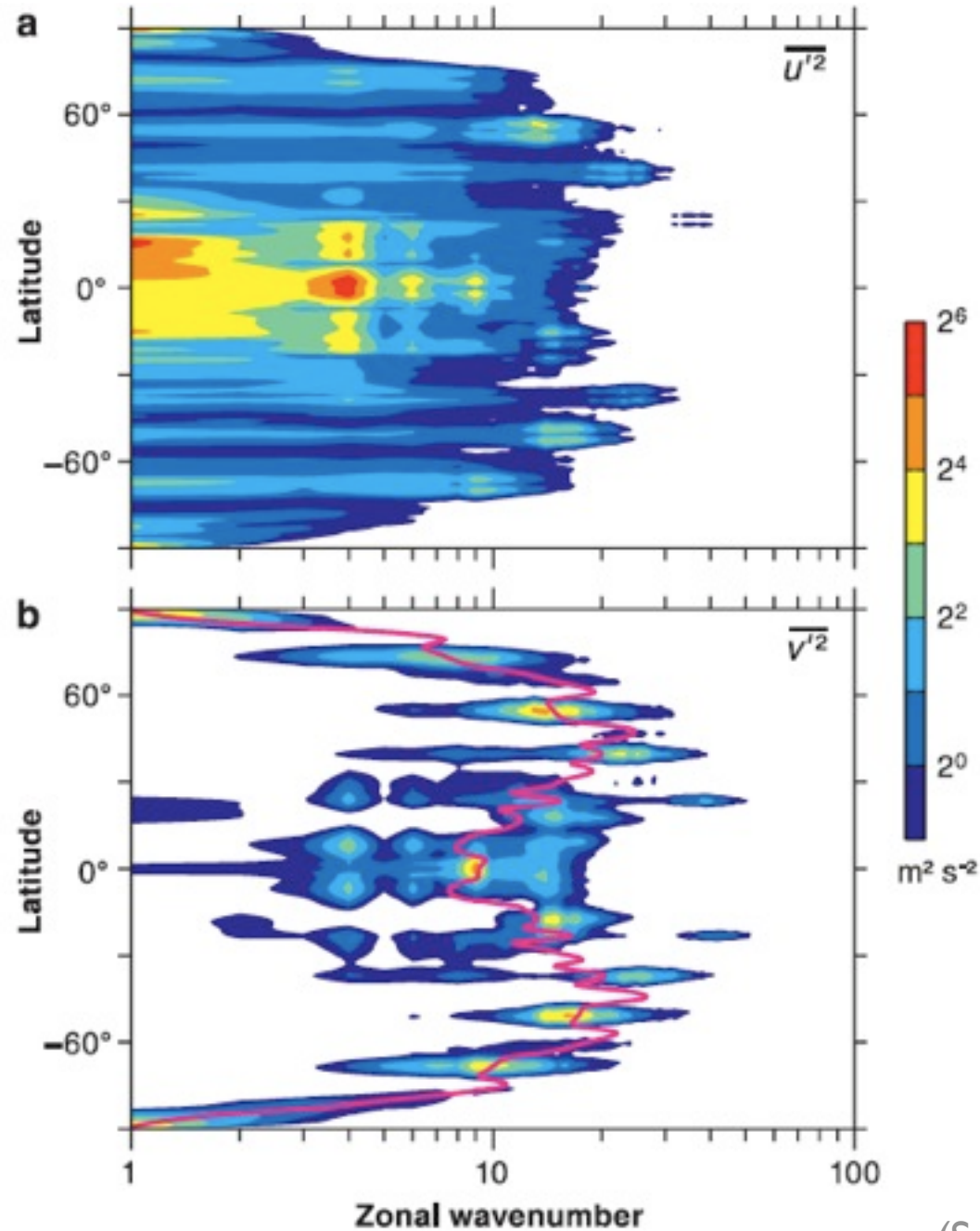


Polar jets and waves



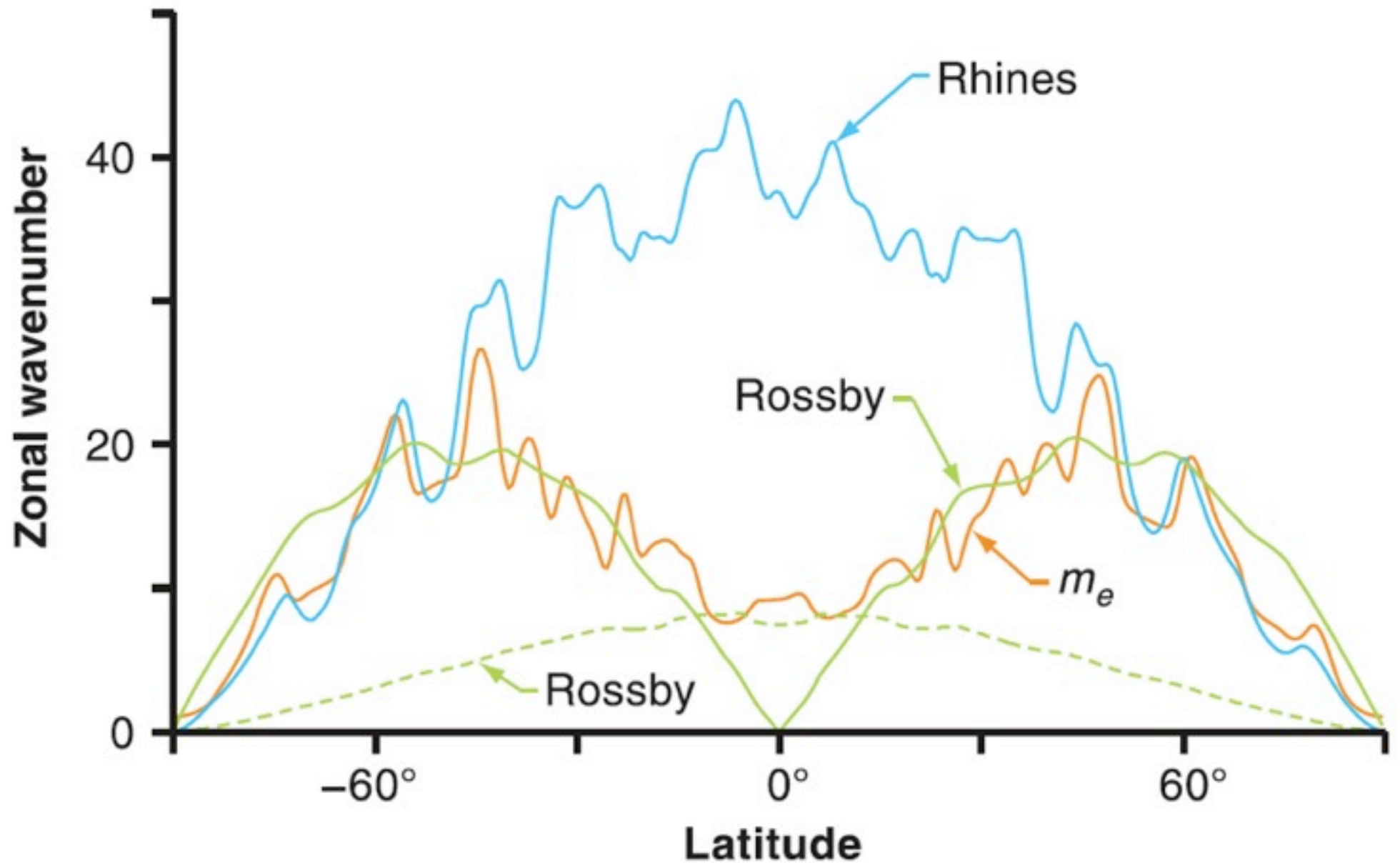
(NASA/JPL, VIMS Team, University of Arizona,
<http://apod.nasa.gov/apod/ap070403.html>)

Velocity variance spectra (Jupiter simulation)



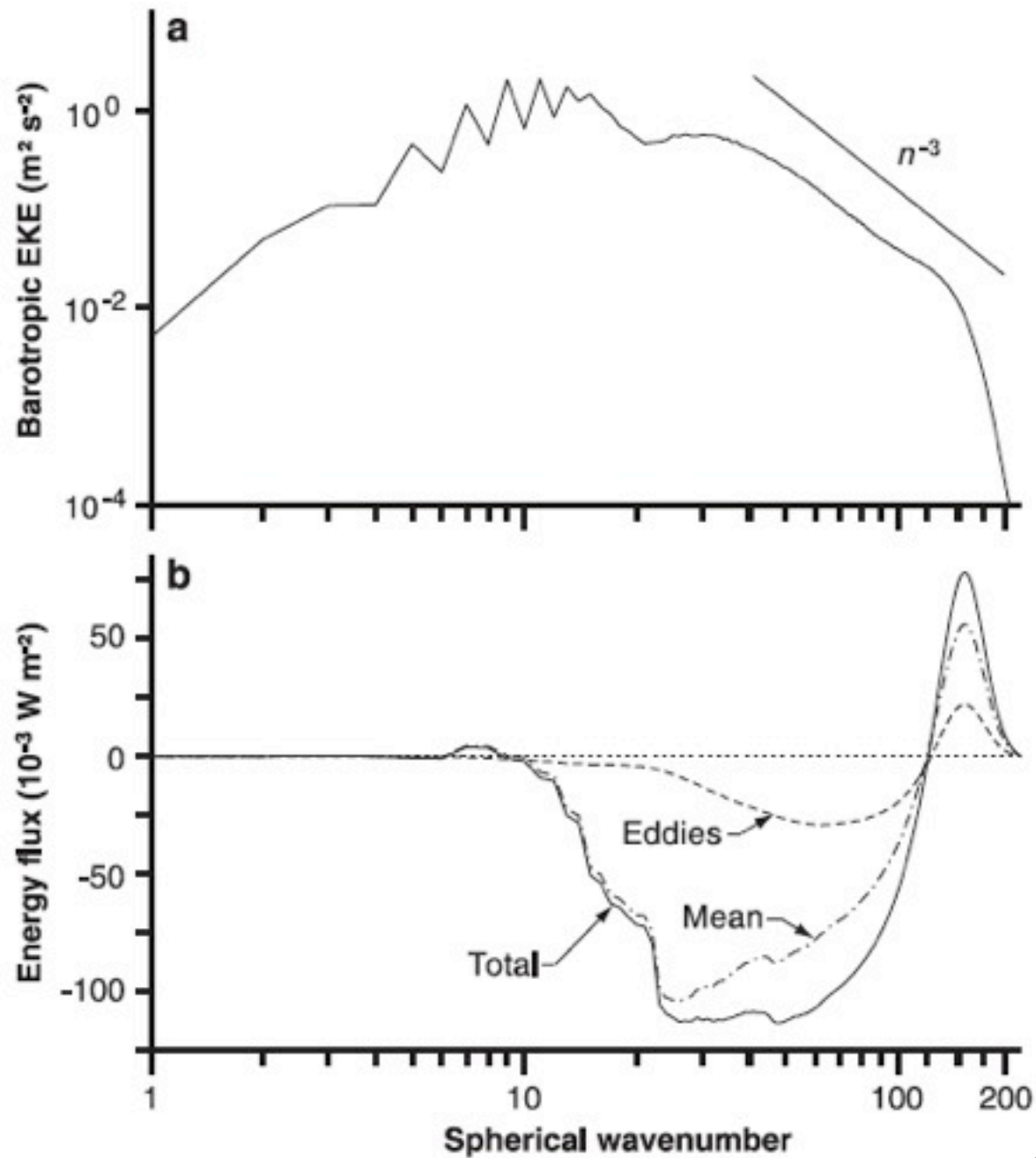
(Schneider & Liu 2009)

Eddy length scales (Jupiter simulation)



(Schneider & Liu 2009)

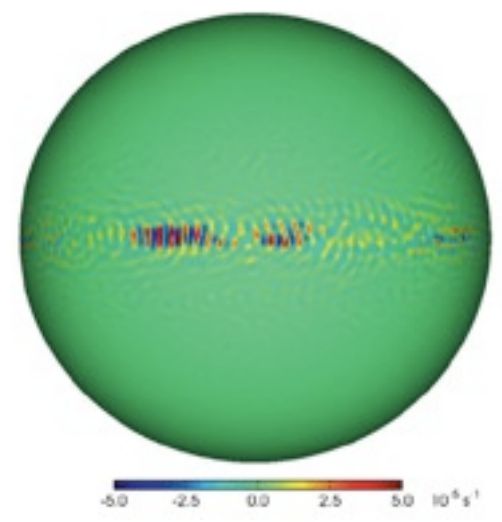
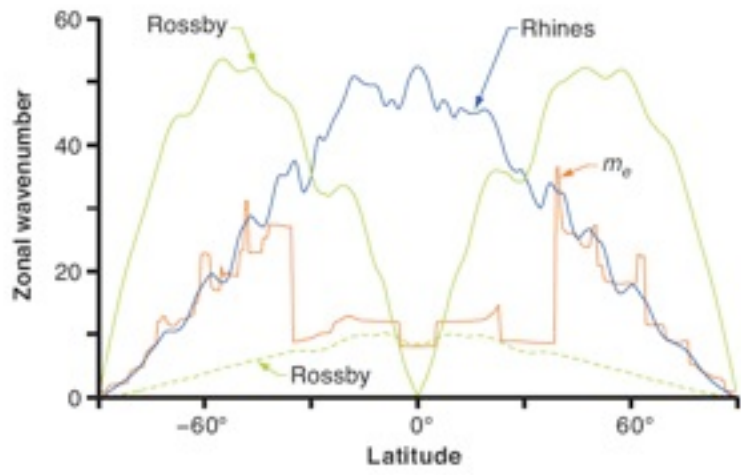
EKE spectrum and flux (Jupiter simulation)



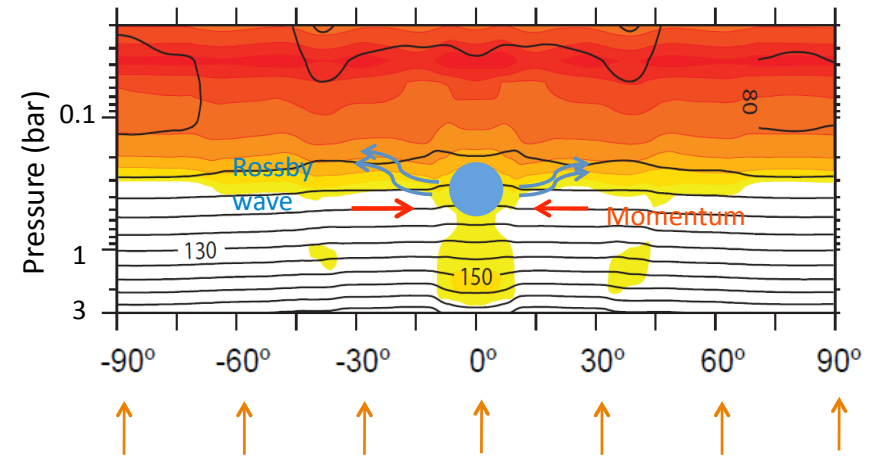
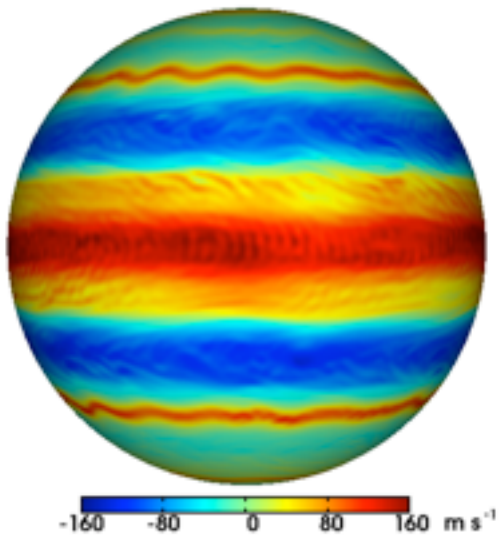
(Schneider & Liu 2009)

Conclusions

- Off-equatorial jets are baroclinically generated; equatorial superrotation generated by convection
- Internal heat flux destabilizes deep layer and increases baroclinicity
- Convection generates equatorial divergence and Rossby waves, leading to superrotation
- Momentum dissipation by coupling to magnetic field at depth
- Strength/scale of jets depends on strength of drag
- No inverse energy cascade necessary



Zonal velocity in Jupiter simulation (100 Earth days)



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